Structural Characterization of Highly Flexible Proteins by Small-Angle Scattering

Tiago N. Cordeiro, Fátima Herranz-Trillo, Annika Urbanek, Alejandro Estaña, Juan Cortés, Nathalie Sibille, Pau Bernadó.

a-Centre de Biochimie Structurale. INSERM U1054, CNRS UMR 5048, Université de Montpellier. 29, rue de Navacelles, 34090-Montpellier, France.
b- LAAS-CNRS, Université de Toulouse, CNRS, Toulouse, France.
c- Department of Pharmacy and Department of Drug Design and Pharmacology, University of Copenhagen, Universitetsparken 2, 2100 Copenhagen, Denmark.

Contact Author: Pau Bernadó (pau.bernado@cbs.cnrs.fr). Tel. +33 467417705

Keywords: Intrinsically Disordered Proteins, Small-Angle X-ray Scattering, Small-angle Neutron Scattering, Ensemble Methods, Protein-Protein Interactions, Nuclear Magnetic Resonance, Low-Complexity Regions, Random Coil Models, Amyloids.
Abstract:
Intrinsically Disordered Proteins (IDPs) are fundamental actors of biological processes. Their inherent plasticity facilitates very specialized tasks in cell regulation and signalling, and their malfunction is linked to severe pathologies. Understanding the functional role of disorder requires the structural characterization of IDPs and the complexes they form. Small-angle Scattering of X-rays (SAXS) and Neutrons (SANS) have notably contributed to this structural understanding. In this review we summarize the most relevant developments in the field of SAS studies of disordered proteins. Emphasis is given to ensemble methods and how SAS data can be combined with computational approaches or other biophysical information such as NMR. The unique capabilities of SAS enable its application to extremely challenging disordered systems such as low-complexity regions, amyloidogenic proteins and transient biomolecular complexes. This reinforces the fundamental role of SAS in the structural and dynamic characterization of this elusive family of proteins.
INTRODUCTION

Intrinsically disordered Proteins or Regions (IDPs/IDRs) have emerged as key actors for a large variety of biological functions such as cell signalling and regulation (Kriwacki et al., 1996; Wright and Dyson, 1999; Dunker et al., 2002; Wright and Dyson, 2015). The main feature of IDPs and IDRs is their lack of permanent secondary or tertiary structure that provides them with an inherent malleability enabling highly specialized biological functions (Dunker et al., 2002). Eukaryotic genomes are highly enriched in genes coding for disordered proteins, and this observation has been linked to the major complexity of these organisms. The capacity of IDPs to adapt their conformation to specifically recognize one or several partners, and the low to moderate affinity for partners make IDPs ideal for protein-protein interactions (Tompa et al., 2015). In fact, it has been shown that interactome hubs are enriched in this family of proteins (Dunker et al., 2005; Kim et al. 2008). Partner recognition is normally performed through conserved and partially structured motifs of the protein, and their individual properties can be modulated by post-translational modifications or alternative splicing. IDRs are highly flexible regions connecting well-folded globular proteins forming the so-called multi-domain proteins. Multi-domain protein topology, which is highly prevalent in eukaryotes, enables the presence of multiple biological activities performed by the globular domains in close proximity (Hawkins and Lamb 1995; Levitt, 2009). In many of these cases, IDRs behave as entropic linkers with an inherent plasticity that can be tuned depending on the length and the specific amino acid sequence of the region.

The biological relevance of IDPs has fostered their structural characterization (Eliezer 2009). Identification of the conformational preferences of binding motifs, the detection of transient long-range contacts within the chain, the structural perturbations exerted by PTM, the shape of biomolecular complexes with disordered partners, and the spatial distribution of globular domains in multi-domain protein are structural features that must be characterized to understand the molecular bases of biological function. This characterization is far from being trivial as the inherent disorder of IDPs/IDRs precludes their crystallization. Nuclear Magnetic Resonance (NMR) has become the only technique that can provide atomic-resolution information on IDPs (Dyson and Wright, 2004). Novel NMR experiments and modelling strategies have been developed to interpret experimental parameters in terms of structure (Jensen et al., 2009; Jensen et al., 2013; Jensen et al., 2014; Wright and Dyson,
2015). However, some structural aspects that remain elusive by NMR such as the overall shape and size of disordered proteins or the distribution of interdomain position in multidomain proteins.

Small-Angle Scattering (SAS) of X-rays (SAXS) or Neutrons (SANS) have emerged as powerful techniques to probe the structure and dynamics of biomolecules in solution at low resolution (Figin and Svergun, 1987; Svergun and Koch, 2003; Koch et al., 2003; Putnam et al. 2007; Jacques and Trehella, 2010). SAS provides unique information about the overall size and shape of individual macromolecules or their complexes in a rapid manner. Additionally, structural changes upon environmental perturbations, such as interactions with other molecules, can be addressed straightforwardly. Major advances in instrumentation and computational methods in the last decade have led to a tremendous increase in the applications of SAS in structural biology (Petoukhov and Svergun, 2007; Mertens and Svergun, 2010; Pérez and Nishioni, 2012; Rambo and Tainer, 2013; Graewert and Svergun, 2013). One of the major advances of SAXS in the last decade has been its extension to address biomolecular dynamics (Doniach, 2001; Bernadó and Svergun, 2012a; Receveur-Brechot and Durand, 2012; Bernadó and Svergun, 2012b; Kikhney and Svergun, 2015; Kachala et al., 2015). Although used in the past to study protein flexibility (Aslam et al., 2003), the availability of robust protocols to interpret SAS data in terms of ensembles of conformations have generalized these studies and, therefore, have enriched the spectrum of applications of the technique (Bernadó and Blackledge, 2010).

The aim of this chapter is to provide an overview of the recent developments of SAS to study highly disordered proteins. A special emphasis is put on biological scenarios involving highly flexible proteins for which SAS is a crucial tool to tackle the structural/dynamic bases of biological function.

**Scattering properties of IDPs**

The fact that IDPs sample an astronomical number of conformations has a strong impact on the scattering profiles measured and their comprehensive analysis in terms of structure. The experimental SAXS profile of an IDP corresponds to the average of all the conformations that the protein adopts in solution, inducing special features to the curves. Figure 1A displays the synthetic SAXS curves for seven conformations of p15PAF, a 111 residue-long IDP, selected from a large pool of 5,000 (De Biasio et al., 2014). The individual conformations display
several features along the complete momentum transfer range simulated. The initial part of the simulated curves, containing the lowest resolution structural information, presents distinct slopes indicating a large variety of possible sizes and shapes that an unstructured chain can adopt. The SAXS profile, obtained after averaging curves for the 5,000 conformations, presents a smoother behavior with essentially no features (Fig. 1B).

Figure 1. (A) Seven representative conformers randomly selected from an ensemble of 5,000 explicit all-atoms models generate for p15PAF (De Biasio et al., 2014). Solid lines correspond to their computed SAXS curves (B) and Kratky plots (C) and are colored as in panel A. T. The average over the ensemble of 5,000 conformations yields a featureless curve that is in very good agreement with the experimental data (gray circles). (D) p(r) functions computed for the 7 conformers and the complete ensembles in the same color code that in panels (A-C).

Traditionally, Kratky plots (I(s)·s^2 as a function of s) have been used to qualitatively identify disordered states and distinguish them from globular particles. The scattering intensity of a
globular protein behaves approximately as $1/s^4$ conferring a bell-shaped Kratky plot with a well-defined maximum. Conversely, an ideal Gaussian chain has a $1/s^2$ dependence of $I(s)$ and therefore presents a plateau at large $s$ values. In the case of a chain with no thickness, the Kratky plot also presents a plateau over a specific range of $s$, which is followed by a monotonic increase. This last behavior is normally observed experimentally in unfolded proteins. The Kratky representation has the capacity to enhance particular features of scattering profiles that allows an easier identification of different degrees of compactness (Doniach, 2001). This is shown in figure 1C where different degrees of compactness for the conformations are observed. Multi-domain proteins present in the same molecule a dual (folded/disordered) behavior consequently SAXS profiles and Kratky plots present contributions from both structurally distinct regions. Pair-wise distance distributions, $p(r)$, derived from disordered proteins also present specific properties (Figure 1D). The most characteristic feature is the smooth decrease towards large intramolecular distances. Maximum intramolecular distance, $D_{\text{max}}$, which represents the maximum distance within one of the accessible conformations of the protein, are very large in disordered proteins. It is worth noting that due to the low population of highly extended conformations in the ensembles, experimental $D_{\text{max}}$ values are systematically underestimated (Bernadó, 2010).

Unstructured proteins, due to the presence of extended conformations, are characterized by large average sizes compared to globular proteins. The radius of gyration, $R_g$, which can be directly obtained from a SAXS curve using a classical Guinier approximation, is the most common descriptor to quantify the overall size of molecules in solution (Guinier, 1939). In the Guinier approximation, it is assumed that at very small angles ($s < 1.3/R_g$) the scattering intensity can be represented as $I(s) = I(0) \exp(-s^2R_g^2/3)$, and the $R_g$ is obtained by a simple linear fit in logarithmic scale. Debye’s approximation (eq. 1) can be more precise than Guinier's one to derive $R_g$ values as its validity extends to larger momentum transfer ranges (Calmettes et al., 1994).

$$\frac{I(s)}{I(0)} = \frac{2}{x^2} \left( x - 1 + e^{-x} \right) ; \quad x = s^2R_g^2$$  \hspace{1cm} (1)

Alternatively, $p(r)$ function calculated from the complete scattering profile using a Fourier transformation also yields precise $R_g$ values for disordered proteins.
The experimental $R_g$ is a single value representation of the size of the molecule, which for disordered states represents a z-average over all accessible conformations in solution (Feigin and Svergun, 1987). The most common quantitative interpretation of $R_g$ for unfolded proteins, which is based on Flory’s studies in polymer science, relates this parameter to the length of the protein chain through a power law (Flory, 1953),

$$R_g = R_0 \cdot N^\nu$$  \hspace{1cm} (2)

where $N$ is the number of residues in the polymer chain, $R_0$ is a constant that depends on several factors, in particular, on the persistence length, and $\nu$ is an exponential scaling factor. For an excluded-volume polymer, Flory estimated $\nu$ to be $\approx 0.6$, and more accurate theoretical estimates established a value of $0.588$ (LeGuillou and Zinn-Justin, 1977). A recent compilation of $R_g$ values measured for 26 chemically denatured proteins sampling broad range of chain lengths found a $\nu$ value of $0.598 \pm 0.028$, and a $R_0$ value of $1.927 \pm 0.27$ (Kohn et al., 2004). The agreement between the $\nu$ value obtained experimentally and the theoretical models suggest the random coil nature of the chemically denatured proteins. However, the question whether the conformational sampling in the chemically denatured state is equivalent to that found for IDPs in native conditions must be clarified (Stumpe and Grubmüller, 2007 and references therein). Using atomistic ensemble models of several disordered proteins, Flory’s equation has been parametrized for IDPs (Bernadó and Blackledge, 2009):

$$R_g = (2.54 \pm 0.01) \cdot N^{(0.522 \pm 0.01)}$$  \hspace{1cm} (3)

The exponential value obtained from the parametrization, $\nu=0.522\pm0.01$, is notably smaller than that derived from the dataset of denatured proteins, $\nu=0.598 \pm 0.028$, indicating that IDPs are more compact than chemically denatured proteins. This observation is in line with NMR studies that indicated that urea denatured proteins have an enhanced sampling (around 15%) of extended conformations compared with IDPs (Meier et al., 2007).
Here, we have collected $R_g$ data from 74 IDPs from the literature (Table 1) that are plotted as a function of the chain length (Fig. 2). As expected, the $R_g$s collected display a correlation with the number of residues of the chain. This linear relationship is closer to the above-mentioned parametrization of IDPs than to that established for chemically denatured proteins. As some IDPs are expected to have certain populations of secondary or tertiary structure, this relationship can be used as an interpretative tool. Thus, deviations from expected IDP random coil model indicate enhanced degrees of compactness or extendedness within the protein.

Figure 2. $R_g$ values from Table 1 (gray dots) as a function of the number of residues are plotted in Log-Log scale. Straight lines correspond to Flory’s relationships parametrized for denatured proteins (blue-dashed) (Kohn et al., 2004) and IDPs (red-solid) (Bernadó and Blackledge, 2009). Colored bands correspond to uncertainty of the parametrization for both models. Some IDPs are not fully disordered and are globally more extended or more compact than expected for a random coil. These structural features even if transient affect the experimental $R_g$. 
Table 1. SAXS studies performed on fully disordered IDPs.

<table>
<thead>
<tr>
<th>Protein</th>
<th>#Residues</th>
<th>(R_g^{exp}) (Å)</th>
<th>(R_g^{RC}) (Å)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>CyaA toxin (1006-1707)</td>
<td>702</td>
<td>84</td>
<td>77.7</td>
<td>(O’Brien et al. 2015)</td>
</tr>
<tr>
<td>MeCP2</td>
<td>486</td>
<td>62.5±4.5</td>
<td>64.2</td>
<td>(Yang et al. 2011)</td>
</tr>
<tr>
<td>Map2C</td>
<td>467</td>
<td>83±1</td>
<td>62.8</td>
<td>(Borysik et al. 2015)</td>
</tr>
<tr>
<td>Rec1-resilin</td>
<td>310</td>
<td>43.4±0.8</td>
<td>50.7</td>
<td>(Balu et al. 2015)</td>
</tr>
<tr>
<td>Msh6 N-term</td>
<td>304</td>
<td>56±2</td>
<td>50.2</td>
<td>(Shell et al. 2007)</td>
</tr>
<tr>
<td>Ki-1/57</td>
<td>292</td>
<td>47.5±1</td>
<td>49.2</td>
<td>(Bressan et al. 2008)</td>
</tr>
<tr>
<td>Juxtanodin (1-282)</td>
<td>282</td>
<td>55.9</td>
<td>48.3</td>
<td>(Ruskamo et al. 2012)</td>
</tr>
<tr>
<td>Dehydrin ERD10 (2-260)</td>
<td>259</td>
<td>60±1.0</td>
<td>46.2</td>
<td>(Borysik et al. 2015)</td>
</tr>
<tr>
<td>MeCP2 (78-305)</td>
<td>228</td>
<td>37.0±0.9</td>
<td>43.3</td>
<td>(Yang et al. 2011)</td>
</tr>
<tr>
<td>PGC-1α 220 (2-220)</td>
<td>219</td>
<td>61.3</td>
<td>42.3</td>
<td>(Devarakonda et al. 2011)</td>
</tr>
<tr>
<td>Synthetic Resilin</td>
<td>185</td>
<td>50±5</td>
<td>38.8</td>
<td>(Nairn et al. 2008)</td>
</tr>
<tr>
<td>CFTR (654-838)</td>
<td>185</td>
<td>32.5±1.8</td>
<td>38.8</td>
<td>(Marasini et al. 2013)</td>
</tr>
<tr>
<td>pCFTR (654-838)</td>
<td>185</td>
<td>29.1±1.8</td>
<td>38.8</td>
<td>(Marasini et al. 2013)</td>
</tr>
<tr>
<td>Dehydrin ERD14 (2-185)</td>
<td>184</td>
<td>60±1.0</td>
<td>38.6</td>
<td>(Borysik et al. 2015)</td>
</tr>
<tr>
<td>Juxtanodin (1-170)</td>
<td>170</td>
<td>42.9</td>
<td>37.1</td>
<td>(Ruskamo et al. 2012)</td>
</tr>
<tr>
<td>Myelin basic protein</td>
<td>170</td>
<td>33</td>
<td>37.1</td>
<td>(Stadler et al. 2014)</td>
</tr>
<tr>
<td>AavLEA1</td>
<td>163</td>
<td>41±1</td>
<td>36.3</td>
<td>(Borysik et al. 2015)</td>
</tr>
<tr>
<td>SRC-1 (617-769)</td>
<td>153</td>
<td>33.96</td>
<td>35.1</td>
<td>(Pavlin et al. 2014)</td>
</tr>
<tr>
<td>Osteopontin</td>
<td>150</td>
<td>37.90±0.08</td>
<td>34.7</td>
<td>(Lenton et al. 2015)</td>
</tr>
<tr>
<td>Pig Calpastatin domain I</td>
<td>148</td>
<td>34.5</td>
<td>34.4</td>
<td>(Konno et al. 1997)</td>
</tr>
<tr>
<td>HrpO</td>
<td>147</td>
<td>35.0</td>
<td>34.4</td>
<td>(Gazi et al. 2008)</td>
</tr>
<tr>
<td>II-1</td>
<td>141c</td>
<td>41.0±1</td>
<td>33.6</td>
<td>(Boze et al. 2010)</td>
</tr>
<tr>
<td>α-Synuclein, pH 7.5</td>
<td>140</td>
<td>40±1</td>
<td>33.5</td>
<td>(Li et al. 2002)</td>
</tr>
<tr>
<td>α-Synuclein, pH 3.0</td>
<td>140</td>
<td>30±1</td>
<td>33.5</td>
<td>(Li et al. 2002)</td>
</tr>
<tr>
<td>N-tail nucleoprotein MV</td>
<td>139</td>
<td>27.2±0.5</td>
<td>33.4</td>
<td>(Longhi et al. 2003)</td>
</tr>
<tr>
<td>β-synuclein</td>
<td>137</td>
<td>49±1</td>
<td>33.1</td>
<td>(Uversky et al. 2002)</td>
</tr>
<tr>
<td>Human NHE1 cdt (5°C)</td>
<td>131</td>
<td>37.1±1</td>
<td>32.4</td>
<td>(Nørholm et al. 2011)</td>
</tr>
<tr>
<td>Human NHE1 cdt (45°C)</td>
<td>131</td>
<td>35.3±1</td>
<td>32.4</td>
<td>(Kjaergaard et al. 2010)</td>
</tr>
<tr>
<td>ERM Transactivation Domain</td>
<td>130</td>
<td>39.6±0.7</td>
<td>32.2</td>
<td>(Lentz et al. 2010)</td>
</tr>
<tr>
<td>Human NL3 (731-848)</td>
<td>118</td>
<td>31.5±1.0</td>
<td>30.6</td>
<td>(Paz et al. 2008)</td>
</tr>
<tr>
<td>elf4E binding Protein (4E-BP)</td>
<td>117</td>
<td>48.8±0.2</td>
<td>30.5</td>
<td>(Gosselin et al. 2011)</td>
</tr>
<tr>
<td>Juxtanodin (172-282)</td>
<td>111</td>
<td>31.5</td>
<td>29.7</td>
<td>(Ruskamo et al. 2012)</td>
</tr>
<tr>
<td>p15c (2-111)</td>
<td>110</td>
<td>28.1±0.3</td>
<td>29.5</td>
<td>(De Biasio et al. 2014)</td>
</tr>
<tr>
<td>Prothromosin α, pH 7.5</td>
<td>109</td>
<td>37.8±0.9</td>
<td>29.4</td>
<td>(Uversky et al. 1999)</td>
</tr>
<tr>
<td>Prothromosin α, pH 2.5</td>
<td>109</td>
<td>27.6±0.9</td>
<td>29.4</td>
<td>(Uversky et al. 1999)</td>
</tr>
<tr>
<td>panNHE1 cdt (5°C)</td>
<td>107</td>
<td>32.8±1</td>
<td>29.1</td>
<td>(Nørholm et al. 2011)</td>
</tr>
<tr>
<td>panNHE1 cdt (45°C)</td>
<td>107</td>
<td>32.9±1</td>
<td>29.1</td>
<td>(Kjaergaard et al. 2010)</td>
</tr>
<tr>
<td>Protein Name</td>
<td>Mw (kDa)</td>
<td>pI</td>
<td>Ref</td>
<td></td>
</tr>
<tr>
<td>--------------------------------------------------</td>
<td>----------</td>
<td>--------</td>
<td>----------------------------</td>
<td></td>
</tr>
<tr>
<td>N-protein of bacteriophage λ</td>
<td>107</td>
<td>33±2 ³</td>
<td>(Johansen et al. 2011a)</td>
<td></td>
</tr>
<tr>
<td>N-protein of bacteriophage λ</td>
<td>107</td>
<td>38±3.5</td>
<td>(Johansen et al. 2011b)</td>
<td></td>
</tr>
<tr>
<td>Human NCBD domain</td>
<td>105</td>
<td>33±1</td>
<td>(Borysik et al. 2015)</td>
<td></td>
</tr>
<tr>
<td>FEZ1 monomer</td>
<td>103</td>
<td>36±1</td>
<td>(Alborghetti et al. 2010)</td>
<td></td>
</tr>
<tr>
<td>HIV-1 Tat₃₃</td>
<td>101</td>
<td>33.0±1.5</td>
<td>28.3</td>
<td>(Foucault et al. 2010)</td>
</tr>
<tr>
<td>Human Calpastatin (137-237)</td>
<td>100</td>
<td>39.0±1.5</td>
<td>28.1</td>
<td>(Borysik et al. 2015)</td>
</tr>
<tr>
<td>p53 (1-93)</td>
<td>93</td>
<td>28.7±0.3</td>
<td>27.1</td>
<td>(Wells et al. 2008)</td>
</tr>
<tr>
<td>Sic1</td>
<td>92</td>
<td>34.7</td>
<td>26.9</td>
<td>(Mittag et al. 2010)</td>
</tr>
<tr>
<td>pSic1 (hexaphosphorylated)</td>
<td>92</td>
<td>34.0</td>
<td>26.9</td>
<td>(Mittag et al. 2010)</td>
</tr>
<tr>
<td>Juxtanodium (103-282)</td>
<td>79</td>
<td>37.4</td>
<td>38.1</td>
<td>(Ruskamo et al. 2012)</td>
</tr>
<tr>
<td>PIR domain</td>
<td>75</td>
<td>26.5±0.5</td>
<td>24.2</td>
<td>(Moncoq et al. 2004)</td>
</tr>
<tr>
<td>N-term NRG1 type III</td>
<td>75</td>
<td>26.8</td>
<td>24.2</td>
<td>(Chukhleb et al. 2015)</td>
</tr>
<tr>
<td>IB5</td>
<td>73 ⁵</td>
<td>27.9±1.0</td>
<td>23.8</td>
<td>(Boze et al. 2010)</td>
</tr>
<tr>
<td>ACTR (5°C)</td>
<td>71</td>
<td>25.8 ⁶ ²</td>
<td>23.5</td>
<td>(Kjaergaard et al. 2010)</td>
</tr>
<tr>
<td>ACTR (45°C)</td>
<td>71</td>
<td>23.8 ⁶ ²</td>
<td>23.5</td>
<td>(Kjaergaard et al. 2010)</td>
</tr>
<tr>
<td>PaaA2 (1-63)</td>
<td>70 ⁵</td>
<td>22.15±0.87 ²</td>
<td>23.3</td>
<td>(Sterckx et al. 2014)</td>
</tr>
<tr>
<td>N-term VS Virus phosphoprotein</td>
<td>68</td>
<td>26±1 ¹</td>
<td>23.0</td>
<td>(Leyrat et al. 2011)</td>
</tr>
<tr>
<td>E3 ubiquitin ligase RNF4 (32-82)</td>
<td>57</td>
<td>25.8</td>
<td>21.0</td>
<td>(Kung et al. 2014)</td>
</tr>
<tr>
<td>Histatin 5</td>
<td>24</td>
<td>13.3</td>
<td>13.3</td>
<td>(Cragnell et al. 2016)</td>
</tr>
<tr>
<td>R/S peptide</td>
<td>24</td>
<td>12.6±0.1</td>
<td>13.3</td>
<td>(Rauscher et al. 2015)</td>
</tr>
</tbody>
</table>

**Constructions of Tau Protein**

<table>
<thead>
<tr>
<th>Protein Name</th>
<th>Mw (kDa)</th>
<th>pI</th>
<th>Ref</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tau ht40</td>
<td>441</td>
<td>65±3</td>
<td>61.0</td>
</tr>
<tr>
<td>Tau K32</td>
<td>202</td>
<td>42±3</td>
<td>40.6</td>
</tr>
<tr>
<td>Tau K16</td>
<td>174</td>
<td>39±3</td>
<td>37.5</td>
</tr>
<tr>
<td>Tau K18</td>
<td>130</td>
<td>38±3</td>
<td>32.2</td>
</tr>
<tr>
<td>Tau ht23</td>
<td>352</td>
<td>53±3</td>
<td>54.2</td>
</tr>
<tr>
<td>Tau K27</td>
<td>171</td>
<td>37±2</td>
<td>37.2</td>
</tr>
<tr>
<td>Tau K17</td>
<td>143</td>
<td>36±2</td>
<td>33.9</td>
</tr>
<tr>
<td>Tau K19</td>
<td>99</td>
<td>35±1</td>
<td>28.0</td>
</tr>
<tr>
<td>Tau K44</td>
<td>283</td>
<td>52±2</td>
<td>48.4</td>
</tr>
<tr>
<td>Tau K10</td>
<td>167</td>
<td>40±1</td>
<td>36.7</td>
</tr>
<tr>
<td>Tau K25</td>
<td>185</td>
<td>41±2</td>
<td>38.7</td>
</tr>
<tr>
<td>Tau K23</td>
<td>254</td>
<td>49±2</td>
<td>45.7</td>
</tr>
<tr>
<td>Tau K32 AT8 AT100</td>
<td>202</td>
<td>41±3</td>
<td>40.6</td>
</tr>
<tr>
<td>Tau ht23 S214E</td>
<td>352</td>
<td>54±3</td>
<td>54.2</td>
</tr>
<tr>
<td>Tau ht23 AT8 AT100</td>
<td>352</td>
<td>52±3</td>
<td>54.2</td>
</tr>
<tr>
<td>Tau K18 P301L</td>
<td>130</td>
<td>35±2</td>
<td>32.2</td>
</tr>
<tr>
<td>Tau ht40 AT8 AT100 PHF1 (10°C)</td>
<td>441</td>
<td>66±3</td>
<td>61.0</td>
</tr>
<tr>
<td>Tau ht40 AT8 AT100 PHF1 (50°C)</td>
<td>441</td>
<td>67±3</td>
<td>61.0</td>
</tr>
</tbody>
</table>
a- When present, purification tags or extra terminal residues resulting from cloning were considered as part of the protein
b- Threshold $R_g$ value obtained from the parametrization of Flory's relationship with the coil database.
c- Length of the most populated isoform of the samples was used.
d- $R_g$ derived from averaging conformations selected with EOM.
e- Data measured by SANS in highly crowded conditions (130 mg/ml of BPTI)
f- Data derived from the 10mM Arg/Glu buffer.
Molecular Modelling of Intrinsically Disordered Proteins

The interpretation of the SAXS parameters such as $R_g$, $p(r)$ and $D_{\text{max}}$ from disordered proteins in terms of structure is limited to overall molecular information. In order to fully exploit the structural and dynamic information encoded in SAXS data, the use of realistic three-dimensional models is necessary. However, the generation of conformational ensembles of disordered proteins is extremely challenging (Zhou, 2004). IDPs present a relatively flat (non-funnelled) energy landscape, with an extremely large number of local minima separated by low-energy barriers. This, combined with their large size, makes the analysis of their energy landscape a challenging problem for computational methods. Most of the available computational methods aim at collecting an ensemble representation of IDPs (Bernadó et al., 2007; Jensen et al., 2014; Wright and Dyson, 2015). This requires an extensive and statistically correct exploration of the conformational space to obtain a representative set of states. Three main families of approaches have been proposed to generate conformational ensembles: molecular dynamics (MD) simulations, Monte Carlo (MC) methods, and experimentally parametrized statistical approaches. These three families of methods are succinctly explained next.

MD simulations analyze the evolution of the system under study by solving Newton’s equations of motion (Karplus and McCammon, 2002; Piana et al., 2014). Theoretically, MD is a suitable method to correctly sample the conformational space of IDPs. Nevertheless, in practice, the high-dimensionality and the wideness of the energy landscape hampers its exhaustive exploration. Several approaches have been proposed to enhance conformational exploration with MD methods. A particularly effective one is Replica Exchange MD (REMD) that runs multiple simulations in parallel with different settings (usually different temperatures) and exchanges states between these processes (Trakawa and Takada, 2011; Zerze GH et al. 2015; Chebaro et al., 2015). Going further in this direction, a very recent method called Multiscale Enhance Sampling (MSES) couples temperature replica exchange and Hamiltonian replica exchange, using a coarse-grained model to guide atomistic conformational sampling (Lee KH et al., 2016). The performance of MD-based method can also be improved by the integration of experimental data to restrain the exploration of the most relevant regions of the conformational space (Lindorff-Larsen et al., 2004; Dedmon et al., 2005; Wu et al., 2009).

MC methods are a classical alternative to MD, being the Markov chain Metropolis scheme
(Metropolis et al., 1953) the most widely used sampling technique (Vitalis and Pappu, 2009). The system is randomly perturbed and the new conformation is accepted with a probability that depends on the energy change between the new conformation and the previous one. Particular mention deserves a recently proposed variant called Hamiltonian Switch Metropolis Monte Carlo (HS-MMC), which has been specially conceived to study IDRs tethered to globular domains. Proteins including IDRs present energy minima due to the contact of the disordered and ordered regions. To avoid being trapped in such minima, the HS-MMC switches between an all-atom Hamiltonian to an excluded volume Hamiltonian to push the IDR away from the ordered domain.

Both, MD-based and MC-based approaches may suffer from inaccuracies of current energy models, which are better suited to globular proteins, and tend to provide structurally biased ensembles that do not properly reflect the conformational behaviour in solution of unstructured proteins (Best et al., 2014; Henriques et al., 2015). The development of more suitable force-fields and solvation models for IDPs are key issues for a correct performance of computational methods (Vitalis and Pappu, 2009b; Emperador et al., 2015).

Knowledge-based statistical approaches are an alternative to physics-based energy functions. The most representative knowledge-based method for the generation of atomistic models of disordered proteins is Flexible-Meccano (FM) (Bernadó et al., 2005; Ozenne et al., 2012), although other similar methods have been described (Jha et al., 2005). The FM algorithm uses an amino acid-specific statistical coil derived from crystallographic structures. In FM, each conformation is built by assembling peptide plane units in a consecutive manner using a residue-specific coil library derived from crystallographic structures. To avoid the collapse of the chain, a coarse-grained description of side chains is also used. Based on this set of conformations, experimentally measurable NMR parameters and SAXS curves can be estimated, which has permitted the validation of the resulting models (see below).

Despite the efforts that have been made to precisely describe the conformational states of disordered proteins, there are still many technical and conceptual issues that must be addressed to correctly describe their energy landscape and, as a consequence, their associated experimental observables.

**Ensemble Approaches**
IDPs sample a large number of conformations. Therefore, ensembles of conformations are the most appropriate framework to structurally represent this family of proteins. In recent years, structural biologists have addressed the challenge of describing dynamic systems in terms of ensembles of reliable conformations guided by experimental data that represents average values for the complete ensemble of conformations (Bernadó and Blackledge, 2010). SAXS has not been exempt from this tendency and several approaches have been developed to characterize protein mobility: Ensemble Optimization Method (EOM) (Bernadó et al., 2007; Tria et al., 2015), Minimal Ensemble Search (MES) (Pelikan et al., 2009), Basis-Set Supported SAXS (BSS-SAXS) (Yang et al., 2010), Maximum Occurrence (MAX-Occ) (Bertini et al., 2010), Ensemble Refinement of SAXS (EROS) (Rozicky et al., 2011), Broad Ensemble Generator with Re-weighting (BEGR) (Daughdrill et al., 2012), and Bayesian Ensemble SAXS (BE-SAXS) (Antonov et al., 2016). These methods are based on a common strategy that consists of three consecutive steps: (i) computational generation of a large ensemble describing the conformational landscape available to the protein, (ii) computation of the theoretical SAXS curves from the individual conformations, and (iii) selection of a subensemble of conformations that collectively describes the experimental profile using multiparametric optimization methods. Despite the common philosophy, these programs present distinct features in the three steps. Readers are referred to the original articles for a detailed description of the approaches.

The availability of ensemble methods has revolutionized the study of flexible proteins by SAS. Ensemble methods provide a description in terms of statistical distributions of structural parameters or conformations that represents a crucial step forward with respect to traditional analysis based on averaged parameters extracted from raw data such as \(R_g\) or \(D_{max}\). In that context, conformational perturbations exerted by temperature (Shkumatov et al. 2011; Kjaergaard et al., 2010), buffer composition (Leyrat et al., 2011), or mutations (Stott et al., 2010) can be monitored in terms of ensembles of accessible conformations.

The main approximation of ensemble methods is the discrete description of entities that probe an astronomical number of conformations. It is therefore reasonable to argue about the real meaning of the SAXS-derived ensembles. An additional problem is the statistically significant size of the derived ensembles based on experimental data with a very limited amount of information (Hammel, 2012; Yang, 2014). The described strategies use distinct philosophies to address these issues. In some cases such as EOM 2.0 and MES, programs
search for the minimal number of conformations required to describe the data to limit or abolish over-fitting. BSS-SAXS and BE-SAXS use Bayesian statistics to address the confidence of the derived populations. In other cases, such as EROS and BEGR, populations of the conformers of an initially built ensemble are slightly modified (re-weighted) in order to describe the data.

SAXS-derived ensembles are representations of the conformational landscape sampled by proteins in solution, but not necessarily the exact states. Ensemble approaches are inherently ill-defined problems, and this is especially severe in SAXS that codes for a very limited amount of structural information. In that sense, it is more adequate to represent highly flexible proteins as distributions of accessible structural parameters such as $R_g$ or $D_{max}$. These representations are less prone to over-fitting artifacts (Bernadó et al., 2007).

In disordered proteins, SAS reports on the overall size and shape of the protein in solution. The presence of extendedness or compactness can be probed by SAS, but regions causing these structural biases cannot be identified unambiguously due to the low-resolution nature of the data. An interesting way to enrich the structural content of SAXS data to more precisely localize partially structured regions in IDPs has been proposed. In this strategy, SAXS curves are measured for multiple deletion mutants of the disordered chain, and simultaneously fitted in terms of a common ensemble. Note that this strategy is only valid if the structural elements of the full-length protein remain intact in the deletion mutants. This approach is described in detail in the original article of EOM where it was applied to a flexible multi-domain kinase (Bernadó et al., 2007). The most notable example of this approach was the study of two isoforms of Alzheimer-related tau, ht23 and ht40 (Mylonas et al., 2008). SAXS data for full-length ht23 and ht40 and for 5 and 3 deletion mutants for each isoform were measured, respectively. The simultaneous fit of all curves with EOM unambiguously identified the so-called repeat region as the source of residual secondary structure in tau. For the ht23 isoform, with three repeats, the maximum separation is found within the repeat domain itself. Conversely, the ht40 isoform, with four repeats, presented an enhanced separation between the repeat domain and the preceding region. These results suggest that the different number of turns (one per repeat) may lead to different global arrangements of the chain in that region.

In addition of the previously described strategy, the information content of SAXS curves measured for IDPs can be enriched with data from other techniques. NMR is by far the most
common technique used synergistically with SAXS (Sibille and Bernadó, 2012), and a special section of this chapter is devoted to it. Additionally, experimental data coming from Electron Paramagnetic Resonance (EPR) and single molecule Fluorescence Resonance Energy Transfer (smFRET) have been synergistically used with SAXS to characterize disordered proteins (Boura et al., 2012). In that sense, the development of robust ways to integrate other biophysical measurements in ensemble approaches is an unavoidable future direction.

**Application of SANS to study IDPs**

The physical bases and the structural information that can be derived form SAXS and SANS are equivalent and, in principle, both techniques can be used to characterize biomolecules. The more general use of SAXS is based on its higher sensitivity and the more widespread availability of beam-lines. SANS however offers some advantages with respect to SAXS. The first one is the absence of radiation damage that makes it a non-destructive technique. The second one is based on the possibility to perform contrast-match experiments, where some components of the sample are made invisible by finely tuning the degree of deuteration of sample components and the ratio of H$_2$O/D$_2$O of the buffer. Contrast matching has been widely used in structural biology and the reader is refereed to the excellent reviews available on the subject (Jacrot, 1976; Heller, 2010; Gabel, 2012).

Although SANS has been used to study IDPs or IDR (Krueger et al., 2011) or radiation sensitive systems (Greving et al., 2010; Stanley et al., 2011; Perevozhikova et al., 2014), its main application is in contrast-match experiments. An example of this family of experiments is the study of the interaction of β-amyloid (1-40) with the detergent SDS (Jeng et al., 2006). In this study the use of deuterated SDS in SANS experiments enabled the characterization of the peptide in the presence of SDS and showed that β-amyloid adopts a short rod-like shape. Interestingly, the authors observed that SDS suppress fibrils by forming complexes with a 30:1 molar ratio between detergent and protein.

IDPs may be particularly sensitive to the effects of molecular crowding, and contrast-matching SANS experiments is a powerful tool to study these effects. By choosing appropriate levels of deuteration of the protein of interest and the crowding agent, the scattering contribution of the latter can be made negligible, enabling the study of the structural perturbations exerted by macromolecular crowding on disordered proteins. This strategy was used to study the disordered N-protein of bacteriophage λ in the presence of
high concentrations of bovine pancreatic trypsin inhibitor (BPTI), a small globular protein (Johansen et al., 2011a; Goldenberg and Argyle, 2014). In 46% D$_2$O, high concentrations of non-deuterated BPTI were contrast matched, and only the signal of the 85% deuterated N-protein was visible. The study demonstrated that molecular crowding exerted a compaction effect on N-protein. However, this effect was non-linear and the effects observed at 65 mg/mL of BPTI were equivalent to those at 130 mg/mL.

**SAXS studies of IDPs within macromolecular assemblies**

Given the structural plasticity of disordered proteins, they are regarded as interacting specialists and have a special place in cell signalling using short motifs or domain-sized disordered segments for partner recognition (Wright and Dyson, 2015; Tompa et al., 2015). Providing a comprehensive description of the biomolecular recognition processes for IDPs is thus of great importance for the understanding of key biological functions that are orchestrated by this family of proteins. In this regard, SAXS is emerging as an extremely valuable tool for characterizing biomolecular interactions involving highly flexible proteins, which are highly challenging for crystallography. The application of solution NMR also encounters severe limitations when characterizing large biomolecular complexes. Conversely, SAXS, which is not limited by size, offers a source of structural and dynamic information that by itself or combined with NMR and/or X-ray crystallography is a promising alternative for the structural characterization of highly dynamic proteins and complexes in solution.

The binding of an IDP to its target produces specific SAXS signatures that enable the detection the interaction. Typically, the mixing of two interacting partners will result in a rise of $R_g$ values, otherwise, if the proteins do not form a complex the $R_g$ value will follow an population-weighted average of the two. Insightful information can be obtained by inspecting the $p(r)$ function in the absence and presence of the disordered interaction partner. The scattering of globular proteins generally give a symmetrical bell-shaped $p(r)$ function, while the interaction with a sufficiently large IDP results in tailing of the peak shape to higher values of $r$, culminating at a large $D_{max}$. The Kratky and Porod-Debye analyses are also powerful indicators of flexibility within macromolecular assemblies (Rambo and Tainer 2011).
It is possible to define 3D molecular envelopes describing the low-resolution shapes of flexible macromolecular assemblies involving IDPs (Longhi et al., 2003; Marsh et al., 2010; Gosselin et al., 2011; Devarakonda et al., 2011). However, the resulting fixed low-resolution structure is not the most appropriate structural description of a disordered protein. Ensemble analysis of explicit or coarse-grained models should provide a more accurate characterization of flexible macromolecular assemblies, particularly if combined with available structure coordinates of folded-domains and data affordable by NMR. Moreover, weak or moderate affinities are a hallmark of many IDP molecular recognition events, which entails the presence of multiple species in solution at standard experimental concentrations. In these cases, any modeling strategy envisioned should account for this species polydispersity to reliably describe SAS data.

Several SAXS studies have been devoted to the interactions of different IDPs with other proteins or DNA, as the only source of structural information or in combination with high-resolution methods. Some examples will be presented.

The complex of Msh2 and Msh6 recognizes mismatched bases in DNA during mismatch repair. The N-terminal region of Msh6, a 304 residue long IDR, recognizes PCNA, a protein that controls processivity of DNA polymerases. Shell and co-workers have demonstrated this direct interaction with SAXS (Shell et al., 2007). A comparison of the $R_g$, Kratky plots and $p(r)$ functions of the isolated partners and the complex showed that PCNA does not induce substantial structure to the N-terminal region of Msh6, which remains mainly disordered and proteolytically accessible upon binding. The interaction of the Msh2-Msh6 complex with PCNA was also addressed by SAXS. The interaction was shown to produce a complex that could be considered as a highly flexible dumbbell where both globular domains are tethered by the N-terminal Msh6 fragment that acts as a molecular leash. These observations were further confirmed in an additional experiment with a biologically active deletion mutant of Msh6 containing a notably shorter N-terminal tail. Under these conditions the important size changes upon binding were easily monitored using the $p(r)$ and $D_{max}$.

The tumor suppressor p53 is a multifunctional protein that plays a crucial role in processes like apoptosis control and DNA repair. P53 is a homotetramer with two folded domains that are tethered and flanked by unstructured regions. Rigid-body modeling of SAXS data measured for p53 suggests that the protein is a rather open cross-like tetrameric assembly,
which collapses to tightly embrace DNA (Tidow et al., 2007). This is how the flexibility of IDPs helps the protein to fulfill its function.

Nuclear receptors (NR) are engaged in gene transcription regulation in response to binding of specific ligands. Signal transduction from ligand binding to gene expression requires the recruitment of co-regulator proteins. Most NR co-regulators function as flexible scaffolds for chromatin modifiers and transcriptional machinery (Millard et al., 2013). Structural analyses of their interaction have been restricted to small peptides of the regulators and the nuclear receptor ligand-binding domain. More recently, several SAXS studies have provided new insights into the stoichiometry and binding mode of the complexes formed by NR and disordered co-regulators (Jin et al., 2008; Rochel et al., 2011; Devarakonda et al., 2011; Pavlin et al., 2014).

β-thymosin/WH2 (β-t/WH2) domains are widespread short disordered regions (25-50 residues) able to recognize G-actin and regulate actin-assembly. When bound to G-actin the N-terminal half of β-t/WH2 adopts a well-ordered amphipathic helix. SAXS analysis at different ionic strengths revealed that the C-terminal regions of different β-t/WH2 domains display distinct dynamics, which correlate with functional differences. At low ionic strength β-t/WH2 sequesters G-actin in a polymerization incompetent state, where the dynamic interactions of the C-terminal part are restrained to a single conformational state. This SAXS-driven observation prompted the study of the β-t/WH2:G-actin complex by NMR at different ionic strengths revealing that a single intermolecular salt-bridge controls the assembly (Didry et al., 2012).

**Low-Complexity Regions**

Low-complexity regions (LCRs) are unusually simple protein sequences with a strong amino acid composition bias, and include homo-repeats of a single amino acid, short period repeats or aperiodic mosaics of a few residues (Wootton and Federhen, 1993). Protein sequences from all three kingdoms of life contain LCRs, but they are more common in eukaryotes, with *Plasmodium falciparum* being an extreme case as ~90% of its proteins host LCRs (Marcotte et al., 1999; Pizzi and Frontali, 2001). Despite their high abundance and doubtless biological relevance, not many studies are focused on the structural characterization of LCRs mainly due to the technical challenges they pose. LCRs are often inserted in IDRs precluding their crystallization (Haerty and Golding, 2010), and the NMR sequence assignment is
complicated (or impossible) by the similarity of nuclear chemical environments. In that context, SAS is a powerful technique to investigate the structure and dynamics of this elusive family of proteins.

Prothymosin α was the first and probably the most well characterized LCR-hosting protein (Gast et al., 1995). Roughly half of the 109 residues of Prothymosin α are acidic (Asp and Glu), leading to a net charge of -44 at neutral pH. A SAXS analysis of prothymosin α at near neutral (7.5) and acidic (2.5) pH showed that while it was unstructured under both conditions, a dramatic reduction in $R_g$ (from 37.8 ± 0.9 Å to 27.6 ± 0.8 Å) could be observed (Uversky et al., 1999). The pH-induced reduction in protein size can be explained by the neutralization of the negatively charged acidic residues due to the decrease in pH. A similar reduction of size was observed after the addition of 15 mM Zn²⁺ at neutral pH ($R_g = 28.1 ± 0.8$ Å) suggesting the electrostatic screening of the negative charges by cations (Uversky et al., 2000). A similar situation was observed for the basic proline-rich salivary proteins IB5 and II-1. Proline-rich salivary proteins bind polyphenolic plant compounds (e.g. tannins) and form aggregates upon binding high concentrations of these compounds. At sequence level IB5 and II-1 contain repetitions of Pro, Gly and Gln or Glu residues, and they are predicted to be disordered. Boze et al. used SAXS to study the conformations of IB5 and II-1, and to see if there are any functional advantages linked to the respective conformations (Boze et al., 2010). Both IB5 and II-1 showed an $R_g$ larger than the theoretical one for IDPs of their lengths, $R_g = 27.9$ Å ± 1.0 Å and 41.0 Å ± 1.0 Å, respectively. In addition, the experimental $D_{max}$ (110 ± 10 Å and 155 Å ± 10 Å, respectively) also indicated the presence of highly extended conformations that could contain poly-proline II helices.

Another example for a protein with low sequence complexity is the crosslinked elastomeric protein resilin. Resilin is rich in Gly, Ser and Pro residues and is present in most insects where it is critical for flight and jumping. Due to its low stiffness, high fatigue lifetime and high resilience, resilin has been of great interest for the production of biomaterials for biomedical applications. SAXS measurements on a recombinant resilin (rec1-resilin) comprising 18 copies of the N-terminal repeat motif (GGRPSDSYGAPGGGN), yielded an $R_g$ of 43.4 ± 0.8 Å and a $D_{max}$ of 200 Å (Balu et al., 2015). Since the expected $R_g$ of a 310 residue-long protein with a compact structure would be ~19.6 Å and that of an IDP would be ~59.5 Å, these data suggest that rec1-resilin is largely unfolded but not completely disordered.
Homo-repeat proteins represent extreme cases for the structural characterization, and huntingtin protein (htt) is the prototypical example of this family of proteins. Htt exon 1 contains two homo-repeat regions consisting of poly-Gln and poly-Pro, respectively. SAXS has been used for the characterization of the overall properties of this protein. Kratky plots of htt exon1 constructs fused to thioredoxin showed broad peaks with less decrease at higher scattering angles, consistent with flexible or unfolded proteins. Interestingly, the observed radii of gyration for constructs with 16 Gln or 39 Gln were very similar, $R_g = 49$ Å or $52$ Å, respectively (Owens et al., 2015). These data were consistent with previous experimental observations and MD simulations indicating that poly-Gln tracts form disordered, collapsed globular structures in solution (Vitalis et al., 2008; Dougan et al., 2009).

An example for a protein with low sequence complexity that forms higher order structures is silk fibroin. The heavy chain of silk fibroin from *Bombyx mori* is 5263 amino acids long and dominated (94%) by the repetition of Gly-X repeats where X is mainly Ala (65%), Ser (23%), or Tyr (9%) (Zhou et al., 2001). In a pioneering study, Greving et al. characterized native (SF) and reconstituted silk fibroin (RSF) by SANS (Greving et al., 2010). Their study identified significant differences between the molecular weights and $R_g$s of native and reconstituted silk fibroin, as well as for RSF samples prepared under different conditions.

**Application of SAS to aggregating IDPs**

Through a complex self-assembly process, some IDPs form amyloid fibrils that are the hallmark of disorders such as Alzheimer’s, Parkinson’s or diabetes (Chiti and Dobson 2006). Fibrillation is a very complex process that involves multiple oligomeric species that are transformed following intricate pathways. Interestingly, there are indications that soluble oligomers, often precursors of fibrils, are the main cause of cytotoxicity and neuronal damage. The structural analysis of the distinct species involved in fibrillation is a major challenge due to their instability, low relative concentration, difficulties of isolation, and the equilibrium between species of very different sizes, present at any time point during the fibrillation process.

The aggregation process of huntingtin exon 1 (htt, see above) has been followed by SANS (Stanley et al., 2011). For this study, the aggregation of a pathological truncated version of the protein encompassing 42 consecutive Gln residues (NtQ_{42}P_{10}) was followed in a time-
dependent manner. The study indicated that the aggregation begins with dimeric and trimeric forms of NtQ_{42}P_{10}. In a very fast process, large oligomeric species, estimated to be 14-mers, are formed, and after that point the protein becomes predominately fibrillar. The same group addressed the effects of the Gln tract length on the fibrillation mechanism by investigating a non-pathological htt version (NtQ_{22}P_{10}) also using SANS (Perevozchikova et al., 2014). Their results indicate that the length of the homo-repeat dictates the size of the initial species and the aggregation pathway followed by htt. In these studies, however, the complex nature of the samples, which are composed by multiple oligomeric species, is not taken into account, and the average values of the derived parameters are analysed. The quantitative interpretation of SAS data of fibrillating proteins requires their decomposition into species-pure SAS profiles, reporting on the structure of each species present, and their relative concentration, reporting on the kinetics of the process. In a pioneering study this challenging SAXS data decomposition was successfully achieved (Giehm et al., 2011). In this study, the fibrillation of α-synuclein was monitored using SAXS by measuring profiles every 30 minutes during 24 hours. Measured profiles contain contributions from all species present at each time-point. Singular Value Decomposition (SVD) analysis indicated that three species are enough to describe the complete SAXS dataset, which were assigned to monomer/dimer, mature fibril, and a third species of unknown nature. Using SAXS profiles measured separately for the two extreme components (monomer/dimer and mature fibril) as fixed contributions, the SAXS curve for the third component was derived (Vestergaard et al., 2007). This decomposed species turned out to be a building block for fibril formation. From the analysis the time-dependent relative populations, the kinetics of the aggregation was also derived. Despite the novelty of the study, it seems clear that more robust and objective approaches to decompose complex SAXS data from aggregating proteins are necessary.

**Combined Use of SAXS and Nuclear Magnetic Resonance**

NMR is the only technique that can provide atomic-resolution information of IDPs (Dyson and Wright, 2004). The first step to study an IDP by NMR is to assign a resonance frequency to all magnetically active nuclei (¹H, ¹⁵N, and ¹³C) of the protein. Due to very low amide proton dispersion, assignment of IDP spectra is challenging. However, the use of high magnetic field spectrometers and several methodological developments allow to routinely
assign NMR frequencies (Narayan et al., 2010). NMR is a highly versatile technique and multiple observables reporting on protein structure and dynamics can be measured. In the following paragraphs the most relevant ones will be succinctly described.

- **Chemical shifts (CSs):** CSs correspond to the resonance frequencies of the nuclei, and are the primary information that can be derived from a NMR experiment. CSs are very sensitive to the chemical environment of nuclei and reveal the presence of secondary structural elements. A chemical shift index (CSI) has been established to highlight regions that deviate from purely random coil to form secondary structural elements (Wishart and Sykes, 1994; Wishart et al., 1995). With the discovery of IDPs, the interest in using CSs to detect partially structured elements has been renewed, and several databases have appeared based on small synthetic peptides (Schwarzinger et al., 2001; Kjaergaard et al., 2011) or IDPs (Tamiola et al., 2010) to identify these regions.

- **Scalar $^3$J$_{HNHA}$ Couplings:** The scalar couplings between H$^N$ and H$^\alpha$ are sensitive to backbone conformations and can be converted into the $\Phi$ torsion angle using Karplus-like relationships (Karplus, 1959). Secondary structures can be unveiled using $^3$J$_{HNHA}$. Values below 5 Hz suggest the presence of $\alpha$-helices, whereas values above 8 Hz suggest extended regions. Values lying in between correspond to random coil conformations. In combination with other NMR observables, $^3$J$_{HNHA}$ can be useful to discriminate between extended structures and poly-proline-II helices (Oh et al., 2012).

- **Residual Dipolar Couplings (RDCs):** RDCs, measured in magnetically aligned samples, are the most sensitive experimental measurement to probe conformational sampling in IDPs (Jensen et al., 2009). Negative NH RDC values are observed in random coil (Louhivuori et al., 2003). Interestingly, more positive and more negative RDCs than expected for a random coil are associated to $\alpha$-helices and extended conformations, respectively (Mohana-Borges et al., 2004). This is an excellent indication to qualitatively assess the presence of distinct types of secondary structural elements. More quantitative interpretation of RDCs can be derived when applying atomistic models of disordered chains (Jha et al., 2005; Bernadó et al., 2005; Marsh et al., 2008). The measurement of multiple backbone RDCs enriches the description of residue-specific structural preferences (Jensen et al., 2008).

- **Paramagnetic Relaxation Enhancement (PRE) experiments:** PREs are measured as enhanced relaxation rates in residues that are close (within 15 to 30 Å) to a paramagnetic tag engineered in a specific position of the chain (Gillespie and Shortle, 1997). Although
nitroxyl spin labels are normally used, paramagnetic cations can also be attached providing, in addition to PREs, other structural observables such as pseudocontact shifts (PCS) (Otting, 2008). PREs are suitable observables to probe transient long-range interactions in IDPs that are manifested when regions of the protein that are far in the sequence form the paramagnetic center present enhanced relaxation phenomena.

The complementarity between NMR and SAS is based on the distinct resolution of the information provided. Whereas SAS probes the overall properties of molecules, NMR information reports on atomic or residue-specific information. Therefore, the simultaneous description of both observables strongly suggests the appropriateness of the derived model.

In that context, SAXS can be used to validate structural models of IDPs refined with NMR data. In this approach, the residue-specific conformational preferences of an IDP are refined using RDCs and CSs using Flexible-Meccano (Bernadó et al, 2005; Ozenne et al., 2012). The final model contains percentages of secondary structural elements in localized regions that have been imposed to properly describe the NMR data. The resulting ensemble can be validated by simply comparing the average SAXS curve computed from the ensemble with that experimentally measured. This strategy has been applied to the partially folded Sendai virus PX (Bernadó et al., 2005), the transactivation domain of p53 (Wells et al., 2008), the K18 construct of Tau protein (Mylonas et al., 2008; Mukrash et al., 2007), and the oncogene p15PAF (De Biasio et al., 2014). A similar approach has been performed to study PaaA2 antitoxin (Sterckx et al., 2014). In this last study the NMR derived ensemble was used as starting pool for a SAXS EOM refinement demonstrating that the protein exists in solution as two preformed helices, connected by a flexible linker.

The best manner to exploit the complementarity of both techniques is to integrate the experimental data into the same refinement protocol. Some of these integrative approaches have been applied to IDPs. One of these is ENSEMBLE, a program that derives ensembles of disordered proteins by collectively describing SAXS curves in addition to several NMR observables: CS, J-couplings, RDCs, PREs, Nuclear Overhauser effects, hydrodynamic radius, solvent accessibility restraints, hydrogen-exchange protection factors, and $^{15}$N R$_2$ relaxation rates (Marsh et al., 2007; Krzeminski et al., 2013). A large number of random structures are computed with FOLDTRAJ or TRADES (Feldman and Hogue, 2000; Feldman and Hogue, 2002), and a Monte Carlo algorithm is used to select a subset of these structures that are collectively consistent with the experimental restraints. This subset is used as a basis for the
generation of new structures, and the process is repeated until a final ensemble consistent with all of the experimental measurements is obtained. This approach addresses the intrinsic problem of under-restraining and consequent over-fitting by finding the smallest ensemble that is consistent with all experimental restraints imposed. ENSEMBLE has been recently applied to characterize the protein Sic1 and its hexaphosphorylated version pSic1 by combining SAXS data with several NMR parameters, including CS, PREs, RDCs, and $^{15}$N R$_2$ (Mittag et al., 2010). Moreover, a structural model of the complex between pSic1, which contains several binding regions, and its partner Cdc4 was generated by combining restraints of the free form of pSic1 with sparse NMR data of the complex suggesting a fuzzy interaction. ASTEROIDS is another program that allows the synergistic interpretation of NMR and SAXS data (Jensen et al., 2008). The power of ASTEROIDS is illustrated in a recent study of tau and α-synuclein using NMR (CSs, RDCs, PREs) and SAXS data (Schwalbe et al., 2014). Using extensive cross-validation, the authors showed that five different types of independent experimental parameters are predicted more accurately by selected ensembles than by statistical coil descriptions. With this method, they could highlight that tau and α-synuclein sample poly-proline II region in the aggregation-nucleation sites.

**Final Remarks**

Disordered systems represent a challenge for structural biology. The presence of multiple conformational states hampers the application of traditional approaches and has fostered the development of strategies with the capacity to capture their inherent plasticity. Despite the limited amount of information coded, SAS has played (and will play) a crucial role in the structural biology of disordered proteins. The appearance of several ensemble approaches to describe SAS data in terms of multiple conformations has been a revolution in the field as they have opened the characterization of the size and shape properties of highly flexible proteins in solution. These methods, however, are model-dependent as their results can be biased depending on the approach used to compute atomic structures of disordered states. New strategies will have to be developed to accurately explore the energetically plausible conformational landscape of disordered proteins without dramatically increasing computational costs. A related aspect that remains poorly understood in IDPs is hydration. The accurate description of surrounding water molecules in disordered chains is necessary to describe their scattering properties.
Alternatively, the integration of experimental information derived from other biophysical methods, mainly NMR, enriches the resolution of the derived conformational ensembles. This is a research field that despite its continuous evolution will require additional efforts. Indeed, a database, pE-DB (http://pedb.vib.be), has been created to compile structural ensembles derived either from NMR, SAXS or their combination to foster integrative approaches and the development of validation strategies in disordered proteins (Varadi et al., 2014).

Disordered biomolecular complexes exemplify the challenges of the field and the need to properly combine experimental and computational approaches. Their characterization requires the detailed description of both the interacting surface and the disordered regions. In that context, SAS can be the key technique to merge in a unified picture the information derived from high-resolution techniques such as NMR and crystallography. Moreover, many of the involving IDPs have a low or moderate affinity causing species polydispersity in typical SAS experiments. This incorporates an additional level of complexity that has to be overcome.

In the last decade there has been a general realization that protein dynamics is fundamental to understand biomolecular function. SAS has a brilliant future in that emerging field. The exploitation of SAS information to address this recent field in structural biology will require further experimental, computational and conceptual developments.

**Acknowledgements**

This work was supported by the ERC-CoG chemREPEAT, SPIN-HD – Chaires d’Excellence 2011 from the Agence National de Recherche, ATIP-Avenir; and the French Infrastructure for Integrated Structural Biology (FRISBI – ANR-10-INSB-05-01) to PB. FHT is supported by INSERM and the Sapere Aude programme SAFIR of the University of Copenhagen. AU is supported by a grant from the Fondation pour Recherche Médicale.
REFERENCES


β-thymosin/WH2 domains controls their functions in actin assembly. EMBO J 31:1000–1013.


Giehm L, Svergun DI, Otzen DE, Vestergaard B (2011) Low-resolution structure of a vesicle


