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Nonlinear control for an uncertain electromagnetic actuator

Flavien Deschaux, Frederic Gouaisbaut and Yassine Ariba

Abstract—This paper presents the design of a nonlinear control law for a typical electromagnetic actuator system. Electromagnetic actuators are widely implemented in industrial applications, and especially as linear positioning system. In this work, we aim at taking into account a magnetic phenomenon that is usually neglected: flux fringing. This issue is addressed with an uncertain modeling approach. The proposed control law consists of two steps, a backstepping control regulates the mechanical part and a sliding mode approach controls the coil current and the magnetic force implicitly. An illustrative example shows the effectiveness of the presented approach.

I. INTRODUCTION

For many years Electro-Magnetic Actuators (EMA) have been developed and used in industrial environment, and especially in automotive industries [1]. This interest can be easily explained by several factors: their small size, their simple structure, their cost/efficiency ratio and the very large range of applications. For example, such technology is used at a micro-scale with the micro-electro-mechanical-systems (MEMS) [2]. At a macro-scale, magnetic bearing systems [3], electromagnetic positioning systems [4] or electronic injection systems of thermal motors [1] are all typical examples of EMA. Also, at a larger scale, this technology is under development for magnetic levitated vehicle [5]. For several years, the National Centre for Space Studies (CNES1) investigates innovative technologies to expand the use of electrical actuators in Ariane launchers. More specifically, the space agency has been working with CSTM, a mechanical engineering company, to replace pneumatic valves with electromagnetic actuators [6]. The present study continues this work, in collaboration with the CNES and CSTM, and focuses on the control issue.

EMA are often controlled by linear control strategies such as Proportional Derivative controller (PD) [7], Proportional Integral Derivative controller (PID) [8] or Linear Parameter Varying (LPV) [9], Model Predictive Control (MPC) [3] and Linear Quadratic Regulator (LQR) controllers [10]. In [7] and [3], a common approximation of the electromagnetic force $F_{\text{mag}} = \frac{N^2 i^2}{k_i}$ is considered. Such simplification may be valid when the magnetic circuit is neglected and only airgap surface are considered. A linearization around a settling point leads to the use of a second order transfer function between the input current and the position of the EMA. In [9] and [10], the expression of the magnetic force has been refined, as $F_{\text{mag}} = N^2 \frac{\dot{i}^2}{(k_0 + k_i \dot{x})^2}$ even though the model is, eventually linearized. In this expression, $F_{\text{mag}}$ depends explicitly on the airgap $x$ and the actuator current $i$. $N$ and $k_i$ are constants related to the physical structure of the system. The nature of this latter expression has led researches to design non-linear control laws.

Hence, in [11], a backstepping approach is proposed to address the stabilization of a nonlinear model of the EMA. Furthermore, a worst-case estimation of the desired magnetic force provides conditions for the backstepping gains to avoid saturation of the magnetic force. However, notice that no explicit analytical model for the electromagnetic force has been developed. Instead, two look-up tables giving the relationships between the magnetic flux, the position and the magnetomotive force on one hand, and between the position, the magnetomotive force and the magnetic force, on the other hand, are used. The approach thus requires finite element method simulation before the control design. In [12], the author uses an adaptive preaction (feedforward) to charge the coil energetically in order to compensate the spring force and a sliding mode control strategy to avoid saturation and achieve a soft landing control. A magnetic equivalent circuit of the actuator is designed in order to evaluate the magnetic force but some terms are neglected like the product between the inductance and the current and the current time derivative $L(t) \frac{di(t)}{dt}$ used in the electrical modeling. [13] combines a linear and nonlinear controls, the magnetic force is regarded as a virtual control input: a linear dynamic output feedback is used to construct the image of the magnetic force needed to stabilize the system and a backstepping method is applied to find the input voltage required. However, the proposed model is simplified and does not contain non-controlled forces like spring force or gravity. [12] and [11] take into account the magnetic saturation phenomenon, but in the literature the flux fringing effect has not been investigated so far.

The flux fringing is a phenomenon that occurs when the magnetic flux flows from a ferromagnetic material to the air. The magnetic flux tends to expand before being canalized again when it flows back through the material. The larger the airgap is, the larger the equivalent surface is. The EMA principle being based on airgap control, if the stroke is significant with respect to the magnetic circuit surface, flux fringing must be taken into account. In control literature, the surface in the airgap is often considered equal to the magnetic circuit surface.

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1The CNES, meaning Centre National d’Etudes Spatiales, is the French space agency.
A first objective of this paper is to consider a more comprehensive model of the actuator and to take into account the flux fringing. The analytical model is derived from a reluctance network approach. This model is then supported by finite element method simulations with COMSOL [14] and electrical system based simulations with PLECS [15]. The effects of flux fringing are then embedded into an uncertain model. Taking into account this issue leads to an uncertain magnetic force, and therefore a non-linear uncertain model. Then a backstepping control cannot compensate a nonvanishing term depending on a spring force. The same applies for the sliding mode, the non-vanishing term does not satisfy the matching condition. The proposed control law is then developed in two steps in order to stabilize the system despite the presence of uncertain parameters. Firstly, the backstepping method is used to stabilize the position and the speed of the moving part of the actuator by computing a suitable coil current signal. Secondly, a sliding mode control is used to control this latter variable. The sliding surface represents the difference between the actual current in the actuator and the desired current for the backstepping control. An illustrative example shows that the proposed approach is able to ultimately bound the EMA despite the model uncertainties.

II. SYSTEM DESCRIPTION AND MODELING

A. Description of the EMA

A schematic representation of the 1-DOF positioning system is shown in Fig. 1. This is a typical setup for electromagnetic valve actuators as presented in [12] and [16]. The electromagnetic system is composed of a multi-turn coil winding a magnetic circuit which is fixed to the frame. A silicon O-ring is installed for limited friction and for sealing. A spring is used to counteract the magnetic force and to ensure that the system returns to the closed position when no supplied.

In order to design a stabilizing control law for the EMA, we firstly develop a nonlinear model, which takes into account some new features like the flux fringing phenomenon. The following three sub-sections will develop the modeling steps to derive a non-linear mathematical model. The EMA will be modeled as a 3 dimensional system with the state vector $x = (x_1, x_2, x_3)^T$. The state components are the position $x_1$ of the mobile part, its velocity $x_2$ and the current of the coil $x_3$. The actuator input $u$ is the voltage at the terminals of the coil.

B. Electromagnetic part

Following [17], the electromagnetic energy is defined by

$$ W_{mag} = \frac{1}{2} L(x_1) x_3^2, \quad (1) $$

where $L$ is the actuator inductance and depends on $x_1$. The magnetic force is therefore:

$$ F_{mag}(x_1, x_3) = \frac{1}{2} x_3 \frac{dL}{dx_1}, \quad (2) $$

Furthermore, the total inductance of the system is defined by [17]:

$$ L = \frac{N^2}{\rho(x_1)}, \quad (3) $$

with $N$ the number of coil’s turn and $\rho(x_1)$ the total reluctance of the magnetic circuit. The reluctance is defined by $\rho = \frac{l}{S \mu}$ [17], where $l$ is the length of the magnetic tube, $S$ its section and $\mu$ the permeability of the material.

Using a finite element method simulation of the magnetic field density in the actuator (Comsol Multiphysics [14]), the path of the magnetic field lines are depicted in Fig. 2.

![Fig. 2. Comsol Simulation - Magnetic field lines](image)

Notice that on Fig. 2, the flux fringing is visible in the airgap: some magnetic field lines do not take the shortest way between the mobile and the fixed part of the EMA. This last figure allows to elaborate an equivalent reluctance network following the magnetic field lines [18] [19]. This network, given in Fig. 3, is composed of six series reluctances delimited by straight sections: three for the body, two for the airgaps and one for the moving part. All physical parameters used to compute the reluctances network are defined in the Fig. 3. This choice of structure leads to a reluctance network depicted in Fig. 3.

Hence, the global reluctance of the system is computed by

$$ \rho(x_1) = \frac{x_1}{\mu_0 S_1(x_1)} + \frac{x_1}{\mu_0 S_3(x_1)} + \rho_0, \quad (4) $$

with $\rho_0$ the sum of the magnetic circuit reluctances, and $\rho_s$ the sum of reluctance that depends on the airgap. The magnetic system of Fig. 3 has been simulated with the electrical engineering software PLECS. For nominal values, the analytical expression of $L$ in equations(3) and (4) has
be estimated as the variable for our model. The second approach approximates the equivalent section by a coefficient such as \( \mu(x_1) \).

Finally, the expression of the magnetic force is obtained by:

\[
F_{\text{mag}}(x_1, x_3) = -\frac{1}{2} x_3^2 N^2 \frac{\rho_x}{\rho(x_1)^2} = -\frac{1}{2} x_3^2 \mu(x_1),
\]

with \( \mu(x_1) = N^2 \frac{\rho_x}{\rho(x_1)^2} \). In the same way as the reluctance \( \rho(x_1) \) and the inductance \( L(x_1) \), define \( \mu(x_1) = N^2 \frac{\rho_x}{\rho(x_1)^2} \) such that \( \mu(x_1) \) is bounded by \( 0 < \mu(x_1) < \mu(x_1) < \mu(x_1) \).

C. Electrical part

Applying the input voltage \( u \) at the terminals of the coil, the electrical dynamic is described by:

\[
u = R x_3 + \frac{d\Phi}{dt},
\]

with \( R \) the coil internal resistance. By definition of the magnetic flux \( \Phi = L x_3 \) we get:

\[
u = R x_3 + \frac{dL}{dt} x_3 + \frac{dL}{dt}.
\]

Since \( \frac{dL}{dt} = \frac{\partial L}{\partial x_1} \frac{dx_1}{dt} \), a dynamical equation for the current \( x_3 \) is formulated as

\[
\frac{dx_3}{dt} = \frac{1}{L(x_1)} \left( u - R x_3 + x_2 x_3 \mu(x_1) \right).
\]

D. Mechanical part

The application of the Newton’s second law to the moving part gives:

\[
m \frac{dx_2}{dt} = -F_{\text{mag}} + F_{\text{ext}},
\]

where \( F_{\text{ext}} \) is the sum of the external forces: \( F_{\text{ext}} = F_{\text{friction}} + F_{\text{spring}} \). \( F_{\text{friction}} \) represents the friction force which is proportional to the speed, \( F_{\text{friction}} = -\lambda x_2 \) and \( F_{\text{spring}} \) is the force due to the spring, proportional to the position, \( F_{\text{spring}} = -K x_1 \) where \( \lambda \) and \( K \) are positive constants.

E. State space model

In this work we consider a 3 dimensional model of the electromagnetic actuator. The state variables have been defined in Paragraph II-A, and gathering equations (8) and (9), a state space model is obtained in (10). Note that the control input \( u(t) \) has effect only on the third equation. We will name \( x_0 \) the initial state of the actuator.

\[
\begin{align*}
\dot{x}_1 &= x_2, \\
\dot{x}_2 &= \frac{1}{m} \left[ \frac{1}{2} x_2^2 \mu(x_1) + F_{\text{ext}}(x_1, x_2) \right] \\
\dot{x}_3 &= \frac{1}{L(x_1)} \left[ u - R x_3 + x_2 x_3 \mu(x_1) \right].
\end{align*}
\]
The proposed method is a combination of a backstepping control and a sliding mode control that makes the closed loop system states converge to a ball around the desired equilibrium point. This equilibrium point depends on the position reference signal \( y_r \) the state \( x_1 \) has to track. The first subsection is dedicated to the design of a backstepping methodology to control the mechanical part of the system. The second subsection develops a sliding mode control to drive the coil current to the required value. Finally, a proof of the system convergence under the proposed control will then be detailed in the third subsection.

The controller design starts by the control of the position and velocity states. The choice of the backstepping method is natural due to the cascade form of the subsystem (11),

\[
\begin{bmatrix}
\dot{x}_1 \\
\dot{x}_2
\end{bmatrix} =
\begin{bmatrix}
1 & \frac{1}{m} \left[ \frac{1}{2} x_{3d}^2 \mu + F_{ca}(x_1, x_2) \right]
\end{bmatrix}
\]

(11)

where \( x_{3d}^2 \) stands for the virtual control input.

**Theorem 1:** Consider \( \alpha_1, \alpha_2 \) two positive scalars, \( a = 1 - \alpha_1 + \frac{\lambda}{m} \) and \( b = \alpha_1 - \frac{\lambda}{m} \). If the matrix \( Q = \begin{bmatrix} -\alpha_1 & a/2 \\ a/2 & b - \alpha_2 \end{bmatrix} \) is negative definite, then the virtual control law \( x_{3d}^2 = -\frac{2m}{\mu(x_1 + y_r)} \alpha_2 (x_2 + \alpha_1 x_1 - \alpha_1 y_r) \) makes the subsystem (11) converge to a ball of center \( \begin{bmatrix} y_r \\ 0 \end{bmatrix} \) and of radius \( \frac{\delta}{\alpha \theta} \), with \( \delta = \frac{K}{m} | y_r |, \alpha = | \lambda_{min}(Q) | \) and \( \theta \) is a positive scalar lower than one.

**Proof:** Consider the classical change of variable

\[
\begin{bmatrix}
z_1 \\
z_2
\end{bmatrix} =
\begin{bmatrix}
x_1 - y_r \\
x_2 + \alpha_1 z_1
\end{bmatrix}
\]

(12)

with \( \alpha_1 \) a positive scalar. The subsystem (11) can be rewritten as:

\[
\begin{bmatrix}
\dot{z}_1 \\
\dot{z}_2
\end{bmatrix} =
\begin{bmatrix}
-\alpha_1 z_1 + z_2, \\
\frac{1}{m} \left[ \frac{1}{2} x_{3d}^2 \mu + F_{ca}(z_1, z_2) \right] + \alpha_1 z_2 - \alpha_2^2 z_1
\end{bmatrix}
\]

(13)

In order to achieve the closed loop desired properties, let us consider a Lyapunov function of the form \( V_1 = \frac{1}{2} z_1^2 + \frac{1}{2} z_2^2 \).

The derivative of \( V_1 \) along the trajectories of (13) leads to:

\[
\dot{V}_1 = -\alpha_1 z_1^2 + a z_1 z_2 + b z_2^2 + 2z_2 \frac{1}{2m} x_{3d}^2 \mu - \frac{K}{m} y_r,
\]

(14)

with \( a = 1 - \alpha_1 + \frac{\lambda}{m} \alpha_1 - \frac{K}{m} \) and \( b = \alpha_1 - \frac{\lambda}{m} \). Consider the control law \( x_{3d}^2 = -\frac{2m}{\mu} \alpha_2 z_2 \) where \( \alpha_2 > | b | \) is a positive scalar. \( \dot{V}_1 \) can then be rewritten as:

\[
\dot{V}_1 = -\alpha_1 z_1^2 + a z_1 z_2 + b z_2^2 + 2z_2 \frac{1}{2m} x_{3d}^2 \mu - \frac{K}{m} y_r,
\]

(15)

with \( z = \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} \) and \( \alpha_1 \) and \( \alpha_2 \) are chosen to obtain \( Q = \begin{bmatrix} -\alpha_1 & a/2 \\ a/2 & b - \alpha_2 \end{bmatrix} \) a negative definite matrix. Therefore,

\[
\dot{V}_1 \leq \lambda_{min}(Q) || z ||^2 + \frac{K}{m} | z_2 | y_r.
\]

(16)

Notice that the term \(-\frac{K}{m} y_r\) can be considered as a nonvanishing perturbation [22] and as \( y_r \) is a bounded signal, there exists \( \delta > 0 \) such that \( | \frac{K}{m} y_r | \leq \delta \). Consider a scalar \( \theta \in [0,1] \), it implies that

\[
\dot{V}_1 \leq -\alpha | || z ||^2 + | z_2 | \delta \\
\leq -(1 - \theta) \alpha | || z ||^2 - \theta \alpha | || z || | || z_2 || \delta \\
\leq -(1 - \theta) \alpha | || z ||^2 \forall | || z || > \frac{\delta}{\alpha \theta}.
\]

(17)

Following [22], the subsystem (11) converges to the disc of center 0 and radius \( \frac{\delta}{\alpha \theta} \) which concludes the proof.

**Remark 1:** As the magnetic force \( F_{mag} \) is uncertain, it cannot compensate exactly the constant term \(-\frac{K}{m} y_r\). The best we can do is to minimize its effect, leading to bound ultimately the subsystem by a small bound [22].

**Remark 2:** A more general Lyapunov function of the form \( V_1 = z^T P z \) may be used in order to reduce the size of the disc. Notice also that an optimization scheme could be implemented in order to minimize the size of the ball in which the states \( (x_1, x_2) \) converges.

The next step of the controller design is to design a control law such that \( x_3 \) converges to \( x_{3d} \). Since the functions \( L(x_1) \) and \( \mu(x_1) \) are uncertain, we rely on a sliding mode approach of order 1 [23].

**Theorem 2:** Consider a scalar \( \varepsilon > 0, \alpha_3 = R | x_{3d} | + | \frac{z_2 - \alpha_1 z_1}{S + x_{3d}} | x_1 + | \frac{z_2 - \alpha_1 z_1}{S + x_{3d}} | \| \| x_1 + \varepsilon, \) the control law \( u = -\alpha_3 \text{sign}(S) \), with the sliding surface \( S = x_3 - x_{3d} \) makes \( x_3 \) converge in finite time towards \( x_{3d} \).

**Proof:** Consider the sliding surface \( S = x_3 - x_{3d} \) and the Lyapunov function \( V_2 = \frac{1}{2} S^2 \). The derivative of \( V_2 \) along the trajectories of (10) leads to:

\[
\dot{V}_2 = S \frac{1}{L(x_1)} u + S \left( \frac{1}{L(x_1)} [ -R(x_3 + x_{3d}) \right.
\]

\[
+ (z_2 - \alpha_1 z_1)(S + x_{3d}) \mu \left. ] - \delta_{3d} \right).
\]

(18)

Let us choose \( u = -\alpha_3 \text{sign}(S) \) with a gain \( \alpha_3 > 0 \) then
\[
\begin{align*}
\dot{V}_2 &= -\alpha_3 |S| \left( \frac{1}{L(x_1)} \right) - R S^2 \frac{1}{L(x_1)} - S \dot{x}_{3d} \\
&+ S \left( \frac{1}{L(x_1)} \right) \left( -R x_{3d} + (z_2 - \alpha_1 z_1) (S + x_{3d}) \mu \right).
\end{align*}
\]

Notice that \( \frac{1}{L(x_1)} \) is an uncertain but strictly positive function and therefore,

\[
\dot{V}_2 \leq |S| \left( \frac{1}{L(x_1)} \right) \left( -\alpha_3 - R x_{3d} + (z_2 - \alpha_1 z_1) (S + x_{3d}) \mu - x_{3d} \dot{L}(x_1) \right).
\]

Setting

\[
\alpha_3 = R |x_{3d}| + |(z_2 - \alpha_1 z_1) (S + x_{3d})| |\mathbf{P}| + |\dot{x}_{3d} | |\mathbf{L}(x_1)| + \varepsilon,
\]

where \( \varepsilon > 0 \), we obtain \( \dot{V}_2 \leq -\varepsilon S = -\varepsilon \sqrt{V}_2 \) which proves the convergence in finite time of \( x_3 \) towards \( x_{3d} \).

The last step consists in proving the convergence of the whole system (10) to a ball around the desired equilibrium point with the control laws defined in Theorem 1 and Theorem 2.

**Theorem 3:** Consider \( \varepsilon_1, \alpha_1, \alpha_2 \) three positives scalars, \( a = 1 - \alpha_1^2 + \frac{k}{m} \alpha_1 - \frac{K}{m} \) and \( b = \alpha_1 - \frac{\lambda}{m} \),

\[
Q = \begin{pmatrix}
-\alpha_1 & a/2 \\
\alpha_2 & b - \alpha_2
\end{pmatrix}, \quad |\lambda_{\min}(Q)| |\alpha_3| = R |x_{3d}| + |(z_2 - \alpha_1 z_1) (S + x_{3d})| |\mathbf{P}| + |\dot{x}_{3d} | |\mathbf{L}(x_1)| + \varepsilon, \quad \text{and} \quad \theta \text{ a positive scalar lower than one.}
\]

If the matrix \( Q \) is negative definite, then the control law \( u = -\alpha_3 \text{sign}(S) \) makes the system (10) convergent to a disc of center \( \begin{pmatrix} y_r \\ x_{3d} \end{pmatrix} \) of radius \( \frac{\varepsilon}{\alpha_3} \), belonging the map \( x_3 = x_{3d} \).

**Proof:** Using \( V = V_1 + V_2 \), we proved in Theorem 1 and Theorem 2 that

\[
V \leq -\alpha \| z \|^2 + \delta \| z \| \| S \| + \frac{\lambda}{m} |S| (x_{3d} + x_{3d}) |P|.
\]

Taking \( \varepsilon = \frac{2}{m} (x_{3d} + x_{3d}) |P| + \varepsilon_1 \) with \( \varepsilon_1 > 0 \)

\[
V \leq -\alpha \| z \|^2 + \delta \| z \| \| S \| - \varepsilon_1 |S|,
\]

\[
\leq -(1 - \theta) \alpha \| z \|^2 - \varepsilon_1 |S|, \quad \forall \| z \| > \frac{\delta}{\alpha \theta}.
\]

As \( S \) converges to 0 in finite time we prove that the whole system converges asymptotically to an invariant and attractive disc of center \( \begin{pmatrix} y_r \\ x_{3d} \end{pmatrix} \) of radius \( \frac{\varepsilon}{\alpha_3} \), belonging the map \( x_3 = x_{3d} \).

**Remark 3:** The proposed approach is a combined backstepping - sliding mode control. Notice that a backstepping approach cannot be applied all along the design due to the nonvanishing term depending on a spring force which cannot be compensated by the control because of the uncertainty. In the same way, it appears to be complicated to design a sliding mode from the beginning because the nonvanishing term does not satisfy the matching condition, the usual condition allowing a sliding mode control to reject a perturbation [23].

**IV. SIMULATION**

Let us consider the EMA whose parameters are given in Table I and consider the control defined by Theorem 3 with the followings parameters \( \alpha_1 = 10, \alpha_2 = 20000 \) and \( \varepsilon_1 = 10 \).

In this simulation, \( y_r \) is a step signal of 3 mm amplitude.

<table>
<thead>
<tr>
<th>Name</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \rho_a )</td>
<td>2.8 \times 10^{-4} H \cdot m^{-1}</td>
<td>Airgap reluctance</td>
</tr>
<tr>
<td>( \rho_b )</td>
<td>630 H \cdot m^{-1}</td>
<td>Magnetic circuit reluctance</td>
</tr>
<tr>
<td>( \lambda )</td>
<td>5 Nm^{-1}</td>
<td>Friction coefficient</td>
</tr>
<tr>
<td>( K )</td>
<td>120 Nm^{-1}</td>
<td>Spring constant</td>
</tr>
<tr>
<td>( N )</td>
<td>70</td>
<td>Coil winding</td>
</tr>
<tr>
<td>( m )</td>
<td>0.1 kg</td>
<td>Mass of the moving part</td>
</tr>
<tr>
<td>( R )</td>
<td>0.4 \Omega</td>
<td>coil intern resistor</td>
</tr>
<tr>
<td>( x_0 )</td>
<td>(0.001 m,0,0)</td>
<td>Initial state</td>
</tr>
</tbody>
</table>

**TABLE I**

The results of the position tracking simulation are shown in the Figure 5, the speed, the current and the input voltage \( u \) respectively in Figures 6, 5 and 7.

Fig. 5. Evolution of the position tracking \( x_1 \) and velocity \( x_2 \)

Fig. 6. Evolution of the coil current \( x_3 \)

The system position follows the reference \( y_r \) with a good settling time (\( \approx 0.2 \)) and no overshoot. There is no chattering on the position and the speed due to the pure integrator in the system. However, a chattering phenomenon appears on the current due to the discontinuous control \( u \). Notice that from a practical point of view, this high frequency switching is not an issue since the implemented control is based on switching transistors. The coil current magnitude is standard as common EMA needs values of a few milliampere.
Fig. 7. Evolution of the voltage input $u$

Fig. 8. Zoom on the tracking error: Plane $z_1 - z_2$

V. CONCLUSION

This paper focuses on a robust control law design for an uncertain model of EMA which takes into account the flux fringing. The proposed control law relies on a combined backstepping and sliding mode control and ensures that the states are ultimately bounded within a disc centered around the reference to be tracked.

Future work consists in, on one hand validating the control law on a testbed, on the other hand, including LMI optimization algorithm in order to minimize the set in which the states converge. In addition, a future work should include the design of a control law taking also into account the magnetic saturation.

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