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# Transition-based RRT for Path Planning in Continuous Cost Spaces

Léonard Jaillet, Juan Cortés and Thierry Siméon

*Abstract*—This paper presents a new method called Transition-based RRT (T-RRT) for path planning problems in continuous cost spaces. It combines the exploration strength of RRTs [1] that rapidly grow random trees toward unexplored regions of the space, with the efficiency of stochastic optimization methods that use transition tests to accept or to reject a new potential state. This planner also relies on the notion of minimal work path that gives a quantitative way to compare path costs. The method also integrates self tuning of a parameter controlling its exploratory behavior. It yields to solution paths that efficiently follow low cost valleys and the saddle points of the cost space. Simulation results show that the method can be applied to a large set of applications including terrain costmap motions or planning low cost motions for free flying or articulated robots.

## I. INTRODUCTION

Sampling-based path planning techniques (see [2], [3] for a survey) have been successfully applied to a large range of problems such as robotics, manufacturing, graphics animation or computational biology. These techniques handle complex problems in high dimensional spaces but usually operate in a binary representation of the search space made up of free regions constrained by obstacles. Due to their probabilistic nature, solution paths are generally low quality and a postprocessing phase is commonly used to improve them relatively to specific criteria, usually the length or the distance to the obstacles. The problem of computing good quality paths with respect to more general cost functions arises in many applications but remains however an open issue.

On the other side, techniques specially developed in the context of field robotics have focused on path planning methods on costmaps [4], where the assigned costs depend on different parameters (eg. robot stability, visibility, probability of presence of an obstacle). Contrarily to sampling based techniques, these methods are however limited to low dimensional problems as they are based on graph search algorithms (eg.  $A^*$  [5] and its dynamic extension  $D^*$  [6]) inside a grid discretization of the space. Few works [7], [8], [9] have recently tried to bridge the gap between sampling based planning and costmap planning. These methods using variants of the RRT diffusion technique [10], focus however on 2D terrain costmap problems.

This paper presents a new technique called Transition-based RRT (T-RRT) for handling more general problems involving continuous cost spaces. This method extends cost planners to higher dimensional problems. More generally

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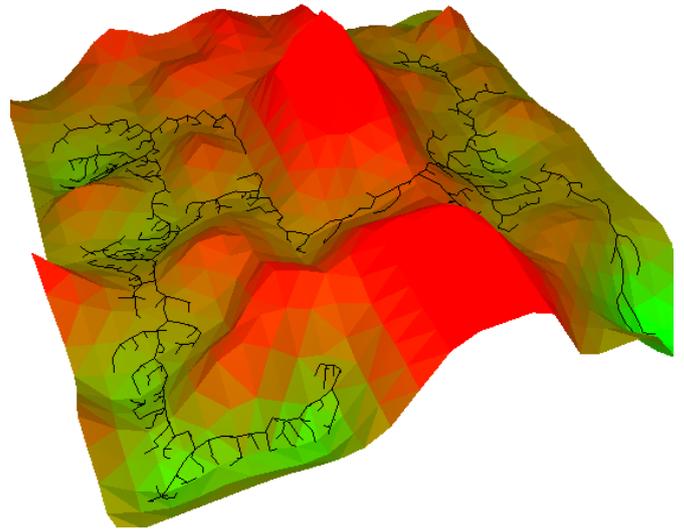


Fig. 1. Transition-based RRT on a 2D costmap (the elevation corresponds to the costs). The exploration favors the expansion in valleys and saddle points connecting low cost regions.

it is applicable to path planning for free-flying or articulated robots in cluttered 3D workspaces, in problems also requiring to integrate some additional cost criterion during the search process in order to compute low cost solution paths. The proposed planner relies on the notion of minimal work path that gives a quantitative way to compare path costs. The algorithm takes advantage of the exploration strength of RRT-like methods that steers the search toward yet unexplored regions of the space, combined with the efficiency of stochastic optimization methods (eg. Monte Carlo optimization, simulated annealing) that use transition tests to accept or to reject a new potential state. This makes the planner follow efficiently valleys and saddle points of the cost space in order to compute low cost solution paths (cf. Figure 1). Finally, the method also integrates self tuning of a parameter controlling its exploratory behavior.

After a brief presentation of the related work (Section II), we introduce (Section III) the minimal work path criterion used to evaluate the path costs. Section IV presents the details of the T-RRT algorithm that is demonstrated in the results (Section V) on different classes of problems involving 2D costmap planning or for computing low cost motions for free-flying and articulated robots.

## II. RELATED WORK

This section briefly surveys the most directly related work to our approach. Only few papers deal with sampling-

based planning and cost spaces. In [7], an adaptation of the RRT-Connect planner is used to find low cost paths in rough terrain applications. The principle is to keep new configurations only if their cost (called *obstacle-ness*) is under a given threshold. This threshold is initialized to a low value, and then iteratively increased during the search process. One limitation of this technique is due to the nondecreasing behavior of this threshold, which limits the efficiency of low cost search to the vicinity of the root nodes. To overcome this issue, the extension proposed in [8], is to grow multiple RRTs rooted at randomly sampled configurations. However, this solution still requires to tune correctly the number of initial samples in order to get sufficient number of low cost seeds among the space. Moreover, it requires a manual tuning of the parameter controlling the cost growth rate that clearly impacts on the algorithm efficiency.

In [9], the heuristically-guided RRT (hRRT) bias the search toward low cost paths using a quality measure based on the cost of the path from the root node and an estimation of the optimal cost to the goal. However such integration of previous costs along a path tends to penalize nodes that are far from the root. In order to balance this behavior, a bias to the goal is performed. The method is developed for 2D applications and only demonstrated on simple examples with discrete cost states (invalid, low cost, high cost). It would probably not be generic enough to succeed in problems involving continuous and higher dimensional cost spaces.

The T-RRT algorithm is also inspired by Monte Carlo optimization techniques. Developed in order to find global optima in very complex function spaces [11], they introduce randomness as a mean to avoid local minima traps. Many variants have been developed (eg. random walk, simulated annealing [12]). The basic exploration process relies commonly on successive transition tests, performed using the Metropolis criterion (see section IV-B). Also note that the Probabilistic Conformational Roadmaps [13] is developed to explore molecular energy landscapes in computational biology applications also integrate a similar transition test in the path planning PRM framework [14].

### III. MINIMAL WORK PATHS

In this section we propose a new criterion to better evaluate path costs. This criterion based on the notion of mechanical work, gives us a quantitative way to compare path qualities.

Let us consider a robot evolving in a configuration space  $CS$  that may contain “binary” obstacles, and a continuous cost function  $c : CS \rightarrow \mathbb{R}^+$  mapping this space, ie. a cost  $c(q) = c_q$  can be computed for each  $q \in CS$ . Consider also a path  $\mathcal{P}$  with a given cost profile corresponding to the various configurations costs along  $\mathcal{P}$ . A positive variation of cost can be seen as a force acting against the motion that produces a mechanical work with the displacement of the robot along the path. The resulting loss of “energy” due to mechanical work is actually the criterion that we propose to minimize. For negative variation of costs, the robot does not loose any

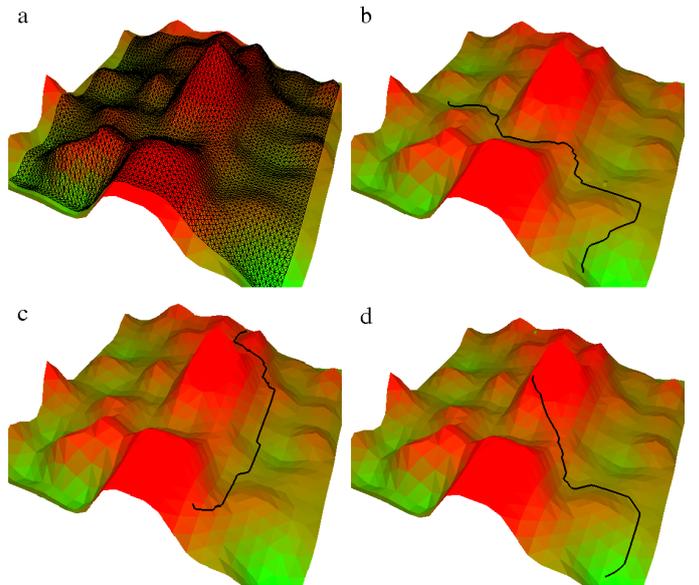


Fig. 2. Optimal paths based on the minimal work criterion. The paths are computed using the  $A^*$  algorithm within a 2-dimensional grid (a) discretizing the space. The examples illustrate respectively down-to-down (b), top-to-top (c), and top-to-down (d) queries.

energy. In that case a small cost proportional to the distance is just added in order to privilege shortest paths. Based on this principle, the cost of a path called  $W(\mathcal{P})$  (in analogy with the mechanical work) can be mathematically expressed as follow:

$$W(\mathcal{P}) = \int_{s_+} \frac{\partial c_+}{\partial s} ds + \epsilon \int_{s_-} ds$$

Here,  $s^+$  represents the path portions with positive slopes, ie. where the cost variations are strictly positive and  $s^-$  the portions where the variations are negative or null.  $\epsilon$  is taken very low compared to the cost values, in order to primarily favor paths with a mechanical work as low as possible and then take among them the paths with decreasing costs portions as short as possible. Then, for a path representation discretized in  $n + 1$  configurations linked by  $n$  edges, we have:

$$W(\mathcal{P}) = \sum_{i \in i_+} (c(q_i) - c(q_{i-1})) d_i + \epsilon \sum_{i \in i_-} d_i$$

where  $i \in i_+$  when  $c(q_i) - c(q_{i-1}) > 0$ ,  $i \in i_-$  otherwise and  $d_i$  is the distance between  $q_{i-1}$  and  $q_i$ .

Figure 2 shows minimal work paths obtained for several queries on a 2D costmap example. For such low dimensional problems, these paths were simply computed using a standard  $A^*$  search performed on a grid discretizing the 2 dimensional landscape. The shapes of the optimal paths are “visually” good, in the sense that they follow as much as possible the low cost regions of the space.

However such grid based planner remains limited to low dimensional problems. The next section introduces the T-RRT algorithm for exploring possibly high dimensional free-space while biasing the search toward low cost regions such

that solution paths remain close to minimal work paths. More generally, the method can also be applied to problems with “binary” obstacles for computing low cost paths according to a given cost function defined over the configuration space (see results provided Section V).

#### IV. TRANSITION-BASED RRT

##### A. General Approach

The main idea of the Transition-based RRT algorithm (T-RRT) is to take advantage of the performance of two methods. First, the exploration strength of RRT-like algorithms resulting from their exploration bias toward large Voronoi regions of the space. Second, the efficiency of stochastic optimization methods developed for computing global minima in complex spaces, and that use transition tests to accept or reject potential states.

Algorithm 1 shows the pseudo-code of the T-RRT planner. Similarly to the *Extend* version of the classical RRT algorithm [15], a configuration  $q_{rand}$  is randomly sampled yielding both to the nearest tree node  $q_{near}$  to be extended and to the expansion direction performed from  $q_{near}$  toward  $q_{rand}$ , with a fixed increment step  $\delta$ .

The increment  $\delta$  is chosen small enough to approximate well the cost variation between  $q_{near}$  and  $q_{new}$ , meaning that linear interpolation does not miss cost picks between the two configurations. Note that in the presence of “binary” obstacles, this stage also integrates some collision detection that rejects the colliding expansion nodes.

---

##### Algorithm 1: Transition-based RRT

---

```

input   : the configuration space  $CS$ ;
           the cost function  $c : CS \rightarrow \mathbb{R}_+^*$ ;
           the root  $q_{init}$  and the goal  $q_{goal}$ ;
output  : the tree  $\mathcal{T}$ ;
begin
   $\mathcal{T} \leftarrow \text{InitTree}(q_{init});$ 
  while not StopCondition( $\mathcal{T}, q_{goal}$ ) do
     $q_{rand} \leftarrow \text{SampleConf}(CS);$ 
     $q_{near} \leftarrow \text{BestNeighbor}(q_{rand}, \mathcal{T});$ 
    if not Extend( $\mathcal{T}, q_{rand}, q_{near}, q_{new}$ ) Continue;
    if TransitionTest( $c(q_{near}), c(q_{new}), d_{near-new}$ )
    and MinExpandControl( $\mathcal{T}, q_{near}, q_{rand}$ ) then
      AddNewNode( $\mathcal{T}, q_{new}$ );
      AddNewEdge( $\mathcal{T}, q_{near}, q_{new}$ );
end

```

---

While this first stage ensures the bias toward unexplored free regions of the space, the goal of the second stage is to filter irrelevant configurations regarding the search of low cost paths before inserting  $q_{new}$  in the tree. As explained in section IV-B, such filtering is performed by the TransitionTest function based on the Metropolis criterion commonly used in stochastic optimization methods.

Additionally, we propose an original way to automatically control the filtering power strength of this test in order to ensure the growth of the tree. Finally, the

MinExpandControl function forces the planner to maintain a minimal exploration rate and thus avoid possible blocking situations during the search. The following subsections details the TransitionTest and MinExpandControl functions.

##### B. Transition Test

The TransitionTest function is presented on Algorithm 2. First, configurations whose cost is higher than the maximal threshold cost  $c_{max}$  are filtered. We then define a probability of acceptance of a new configuration by comparing its cost  $c_j$  relatively to the cost  $c_i$  of its parent configuration. This transition test is based on the Metropolis criterion. The transition probability  $p_{ij}$  (referred as the Boltzmann probability when applied to statistical physics or molecular modeling) is defined as follow:

$$p_{ij} = \begin{cases} \exp\left(-\frac{\Delta c_{ij}^*}{K * T}\right) & \text{if } \Delta c_{ij}^* > 0 \\ 1 & \text{otherwise.} \end{cases}$$

with:

- $\Delta c_{ij}^* = \frac{c_j - c_i}{d_{ij}}$ , the slope of the cost, ie. the cost variation divided by the distances between the configurations. Thus, downhill transitions are automatically accepted whereas for uphill transitions, those with the steepest slopes have the lowest chances to be accepted.
- $K$  is a constant value used to normalize the cost variations, simply determined by the average cost of query configurations  $K = \frac{c_{init} + c_{goal}}{2}$ .
- $T$  is a “temperature” parameter that controls the difficulty level of transition tests.

1) *Temperature Parameter*:  $T$  is an important parameter of the algorithm since low temperatures limit the expansion to low positive slopes. On the contrary, higher temperatures permit expansion on higher slopes. Among the various applications of the Metropolis criterion, the temperature can be kept constant (eg. Monte Carlo search) or decreased gradually as the search progresses (eg. simulated annealing).

2) *Adaptive Tuning*: The TransitionTest function performs an adaptive tuning of the temperature during the search process (second stage of Algorithm 2). At the initialization of the algorithm,  $T$  is first set to a very low value (eg.  $10^{-6}$ ) in order to only authorize very low positive slopes (and negative ones). Then, during the exploration, the number  $nFail$  of consecutive times the Metropolis criterion discards a configuration is memorized and used for temperature tuning. When the T-RRT search reaches a maximal number of rejections  $nFail_{max}$ , then the temperature is multiplied by a given factor  $\alpha$ . On the contrary, each time the tree successes to climb a slope, the temperature is divided by the same factor  $\alpha$ . Proceeding in this way, the temperature automatically adapts itself such that in average a new node climbing a slope is inserted every  $nFail_{max}$  times. For all our experiments, we have taken  $\alpha = 2$  and  $nFail_{max} = 100$ .

##### C. Minimal Expansion Control

The adaptive temperature tuning introduced above for the transition tests ensures a given rate of slope climbing

---

**Algorithm 2:** TransitionTest( $c_i, c_j, d_{ij}$ )

---

```
begin
  if  $c_j > c_{max}$  then return False;
  if  $c_j < c_i$  then return True;
   $p = \exp(\frac{-(c_j - c_i)}{K * T})$ ;
  if  $Rand(0, 1) < p$  then
     $T = T / \alpha$ ;
     $nFail = 0$ ;
    return True;
  else
    if  $nFail > nFail_{max}$  then
       $T = T * \alpha$ ;
       $nFail = 0$ ;
    else
       $nFail = nFail + 1$ ;
    return False;
end
```

---

successes. However in some cases, a possible side effect can be a too slow expansion of the tree versus an excessive refinement of explored regions. We further discuss below this issue and explain how the `MinExpandControl` function overcomes this problem.

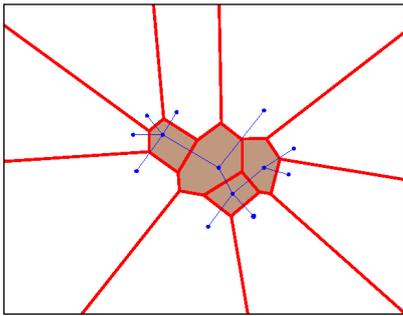


Fig. 3. *Frontier* nodes (white regions) have a Voronoi region bounded by the space limits contrarily to *non frontier* nodes with a Voronoi region bounded by the Voronoi region of other nodes (brown/gray regions). The distinction of these 2 types of nodes is specially useful in the case of cost spaces.

1) *Exploration versus Refinement*: The behavior of the RRT expansion can be explained by distinguishing two types of nodes [16]: *frontier* nodes (with a Voronoi region bounded by the space limits) and *non frontier* nodes (with Voronoi region entirely bounded by the Voronoi region of the other nodes). Whereas the extension of a *frontier* node tends to explore new regions of the space, the extension of *non frontier* nodes only leads to the refinement of the existing tree (see Figure 3). In the case of the T-RRT method, it happens that whereas the temperature needs to grow in order to develop *frontier* nodes and make the tree explore new regions, it is stabilized by the insertion of *non frontier* nodes refining the tree in easier regions of the space. The problem of unbalanced refinements and explorations modes was already addressed in [16], [17] for standard RRTs. However the problem with T-RRT is different since the insertion of refinement nodes directly

impacts on the temperature and thus on the probability to create new exploration nodes. Figure 4 illustrates this issue with an example of tree (left) whose expansion has been stopped by the too frequent insertion of *non frontier* nodes. It also shows the solution to the problem obtained using the minimal expansion control that is detailed below (right).

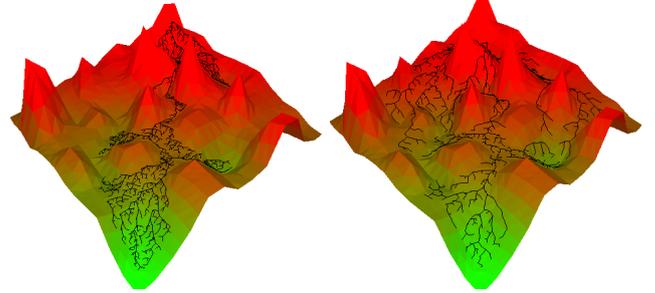


Fig. 4. Impact of the minimal expansion control on the T-RRT algorithm. Without control (left), the insertion of refinement nodes tends to slow down the exploration by decreasing the temperature. By performing this control, the planner is forced to keep exploring new regions of the space.

2) *Minimal Exploration Rate*: The proposed solution is to force the planner to keep exploring new regions of the space by controlling the ratio between exploration and refinement steps. It is important to note that *non frontier* nodes have a Voronoi region usually much smaller than the one of *frontier* nodes (bounded by the Voronoi regions of other nodes). Based on this property, extension steps can be estimated as refinements or expansions in function of the distance between  $q_{near}$  and  $q_{rand}$  (the rationale is that a small distance corresponds to configurations having a higher probability to be *non frontier* nodes). In practice,  $q_{new}$  is considered as participating to the tree expansion if this distance is higher than the expansion step  $\delta$ . On the contrary,  $q_{new}$  is supposed to participate to the tree refinement when the distance is lower than  $\delta$ . The control of minimal exploration rate is performed by the `MinExpandControl` function that rejects configurations accepted by the transition-based test if they make the ratio between exploration and refinement mode lower than a given minimal value (set to 1 in our implementation).

## V. EXPERIMENTAL RESULTS

The basic Extend-RRT algorithm and its T-RRT variant have been implemented into the path planning software *Move3D* [18]. The experiments reported below were performed on a 1GHz AMD Opteron 148 processor. All performance results summarized in the tables correspond to average values computed over 10 runs.

The first set of experiments evaluates T-RRT in the case of a 2-dimensional cost space (Figure 5). In this example, the solution paths have to get through a saddle point to link the query configurations located at two opposite corners of the environment. The figure shows snapshots of the exploration tree during the search process and the solution path found

TABLE I

2D COST SPACE, COMPARATIVE RESULTS FOR RRT, T-RRT ( $nFail_{max} = 100, 10$ ) AND THE OPTIMAL PATH  $\mathcal{P}^*$ .

	$length$	$c_{min}$	$c_{max}$	$c_{ave}$	$W$
RRT	148	8	36	21	<b>32.7</b>
T-RRT	214	8	23	17	<b>19.5</b>
T-RRT <sub>10</sub>	182	8	25	18	<b>21.9</b>
$\mathcal{P}^*$	178	10	23	17	<b>13.3</b>

(bottom-left) which is close to the optimal one (bottom-right). Path qualities using T-RRT are compared in Table I to those using a basic RRT algorithm and to the optimal path  $P^*$  computed with an  $A^*$  search within a  $128 \times 128$  grid discretizing the space.

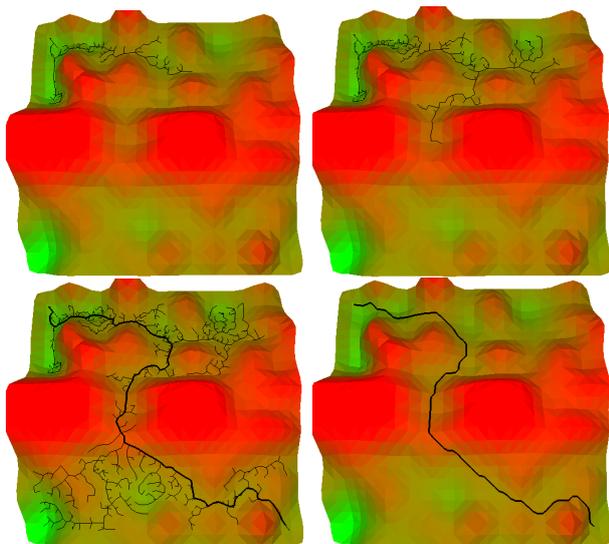


Fig. 5. Expansion process of the Transition-based RRT finding a low cost solution path (bottom-left), close to the optimal one (bottom-right) computed from a space discretization.

Solution paths for the classic RRT algorithm (almost straight line paths) are 2.5 times more costly than the optimal solution path (32.7 vs. 13.3). In comparison T-RRT path costs are only 45% higher than the optimal one. Most importantly, the overall shape of solution paths is very close to the optimal one and follows the same low cost regions. Therefore, a simple post processing (local optimization) would certainly be sufficient to tend toward the optimal solution path. Concerning the influence of the  $nFail_{max}$  parameter, note that a smaller value ( $nFail_{max} = 10$  instead of 100) yields to very similar solution paths with slightly higher costs, but balanced by a large improvement of computing time performance (1.4s vs. 28.6s).

Next experiments illustrate the generality of the algorithm, which is not limited to 2D costmap planning, but also able to integrate cost functions for planning motions of more complex robot systems. First example involves a 6-dof manipulator arm carrying a rod in 3D environment cluttered with obstacles (see Figure 6). The goal of the planner is

to extract the rod from a hole, keeping it as far as possible from the obstacles. Thus the cost function considered for this case corresponds to the inverse of the distance of the rod to the obstacles. Results are presented on Table II. The cost of solution paths found with T-RRT are considerably lower than the ones found with RRT (with respective computing times of 19.2s and 3.3s). This difference of quality is much higher here since there is no limitation on the cost function (contact configurations have an infinite cost) contrarily to the costmap example of Figure 5. The last row of Table II illustrates an interesting feature of T-RRT. The standard deviation  $\sigma_W$  computed over the solution path costs shows the regularity of the paths costs obtained with the T-RRT method. Contrarily to the erratic motions of the classical RRT, T-RRT paths tends to keep the rod horizontal during its extraction from the hole in order to stay at a fixed maximal distance from the obstacles.

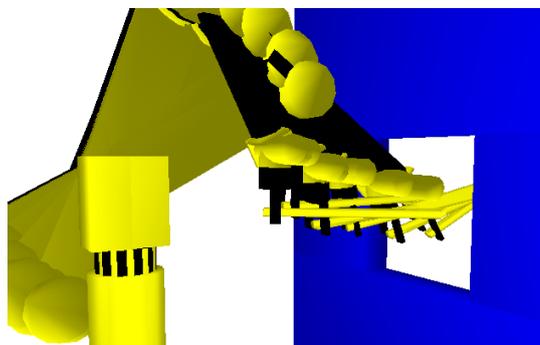


Fig. 6. 6-dof manipulator arm extracting a rod from a hole thanks to the T-RRT planner. The solution path tends to keep the rod horizontal during the motion in order to stay as far as possible from the obstacles.

TABLE II

6-DOF MANIPULATOR ARM WITH BINARY OBSTACLES, COMPARATIVE RESULTS FOR RRT AND T-RRT.

	$length$	$c_{min}$	$c_{max}$	$c_{ave}$	$W$	$\sigma_W$
RRT	45	0.1	17150	88	<b>3279</b>	3151
T-RRT	49	0.1	40.4	1	<b>15.2</b>	5.22

Last experiment was performed on the molecular model shown Figure 7. The task is to compute the pathway extracting the ligand (small molecule in red/dark) from the active site located inside a protein. This problem can be seen as a mechanical disassembly path planning problem for the free-flying ligand [20]. Energetic constraints are translated into geometric ones by considering a steric model of the molecules and applying a collision detection [19] as a geometric filter that rejects conformations with prohibitively high van der Waals (VdW) energy. Like for the manipulator example, the cost function considered in this case is defined as the inverse of distance between the ligand and the protein. The interest of this molecular model is to provide a simple way to quantify the quality of the solution path. Hence, a dilatation of the ligand free space can be simply obtained by shrinking the atoms radii. The results reported in Table III

TABLE III  
LIGAND-PROTEIN EXAMPLE WITH AN INITIAL VdW RATIO OF 25%,  
COMPARATIVE RESULTS BETWEEN RRT AND T-RRT.

	$length$	$c_{min}$	$c_{max}$	$c_{ave}$	$W$	$VdW_{max}$
RRT	59	0.1	2236	14	<b>471</b>	0.25
T-RRT	70	0.1	1.0	0.3	<b>0.3</b>	0.66

were obtained by applying both RRT and T-RRT algorithms on the shrunk model shown in the right image in Figure 7 (25% of VdW radii). T-RRT solution path has a much lower cost compared to the one computed by RRT. The higher clearance of the T-RRT solution is also quantified by the maximal VdW ratio indicated in the last row of the table. This maximal ratio was simply obtained by testing solution paths with VdW radii increasingly grown until a collision was detected between the ligand and the protein. While no growing was possible for the RRT solution, the T-RRT path (computed with a 25% ratio) remains valid up to 66%, which is relatively close to the maximal value allowing the ligand to exit (80%). This high clearance of the T-RRT computed path shows its good quality with respect to the distance-based cost considered for this example.

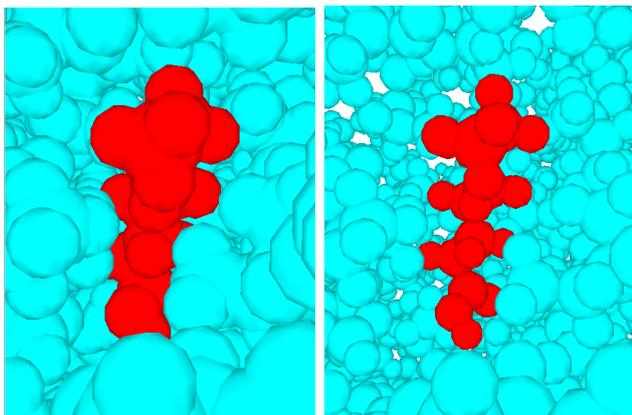


Fig. 7. Two representations of the same ligand protein problem, with different van der Waals radii: maximal radius (left) and shrunk radius (right).

## VI. CONCLUSIONS AND FUTURE WORKS

We have presented the Transition-based RRT algorithm (T-RRT) that takes advantage of both the exploration strength of the RRT and the efficiency of stochastic optimization methods. It integrates a self tuning of the temperature parameter to adapt the difficulty of the transition tests in function of failures and successes during the search process. An explicit definition of the optimality criterion allows us to compare solution path with the optimal ones and helps us to quantify the experimental results. The algorithm is general enough to be applied to high-dimensional spaces also constrained by obstacles or to classical costmaps in rough terrain applications.

The first simulation results reported in the paper show the effectiveness of the method for solving both classes of

problems. However there remain several possible improvements, in particular to consider higher dimensional problems or to increase the optimality with some postprocessing of the T-RRT computed path. We also plan to investigate possible applications of the technique: the integration of human-robot interaction constraints into computed motions and also the exploration of energy landscapes in computational biology problems.

## VII. ACKNOWLEDGMENTS

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